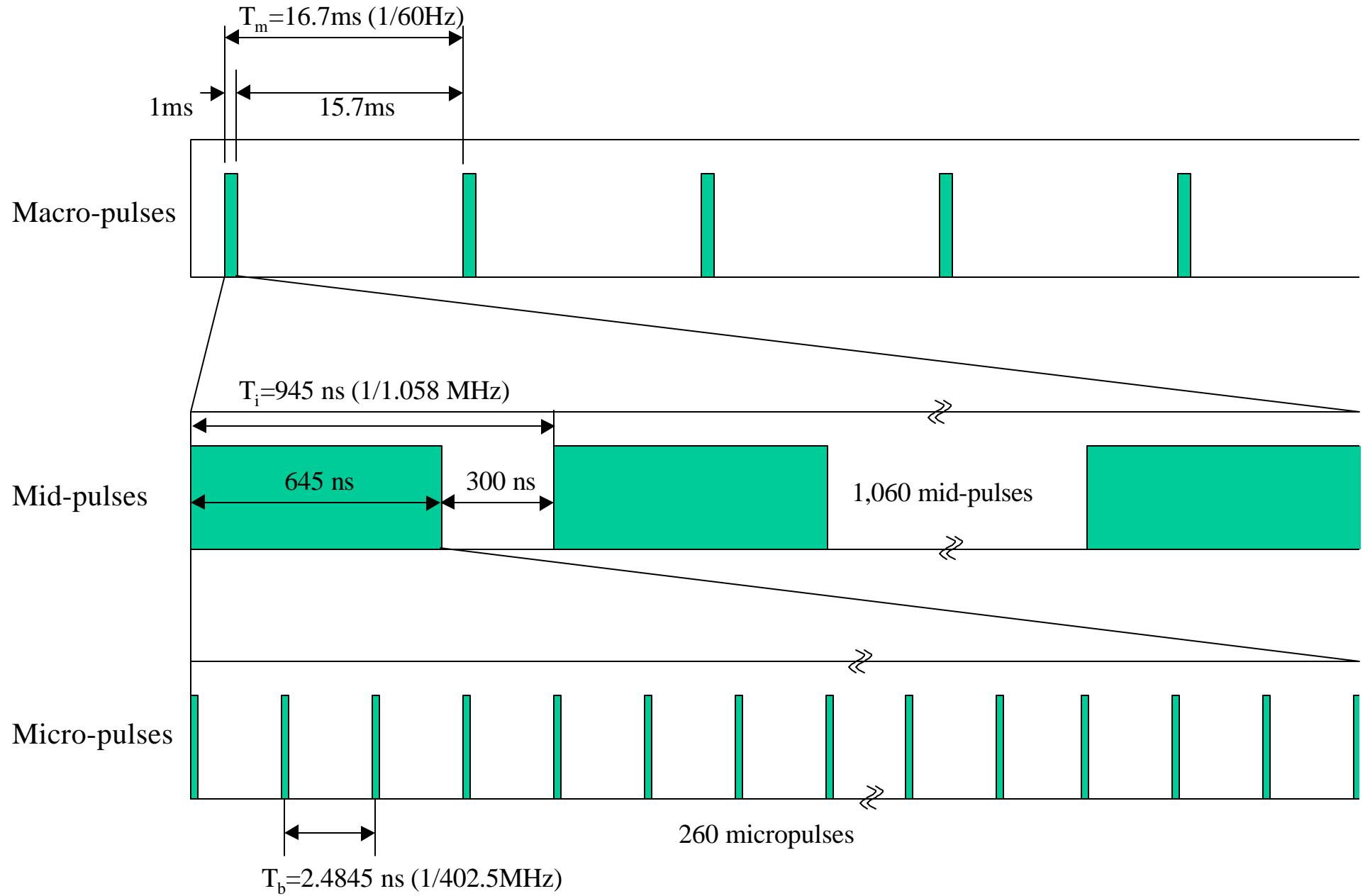


Time structure of SNS beam



HOM Power

Each HOM Power excited by beam

Power to the HOM coupler

$$P_{\text{HOMn,coupler}} = (\pi f_n I_0 T_b)^2 (R/Q) F^2 / Q_{\text{ex}}$$

f_n ; HOM frequency,

I_0 ; beam current (52 mA during the mid pulse)

T_b ; micro bunch distance (1/402.5MHz)

R/Q ; HOM R/Q

Q ; quality factor of cavity (intrinsic)

F; multiplication factor of spectral lines (from time structure)

Q_{ex} ; HOM external Q

Each HOM Power dissipation on the cavity wall

$$P_{\text{HOMn,c}} = P_{\text{HOMn,b}} Q_{\text{ex}} / Q = P_{\text{HOMn,b}} / (1 + \beta) \approx P_{\text{HOMn,b}} / \beta$$

β ; coupling constant

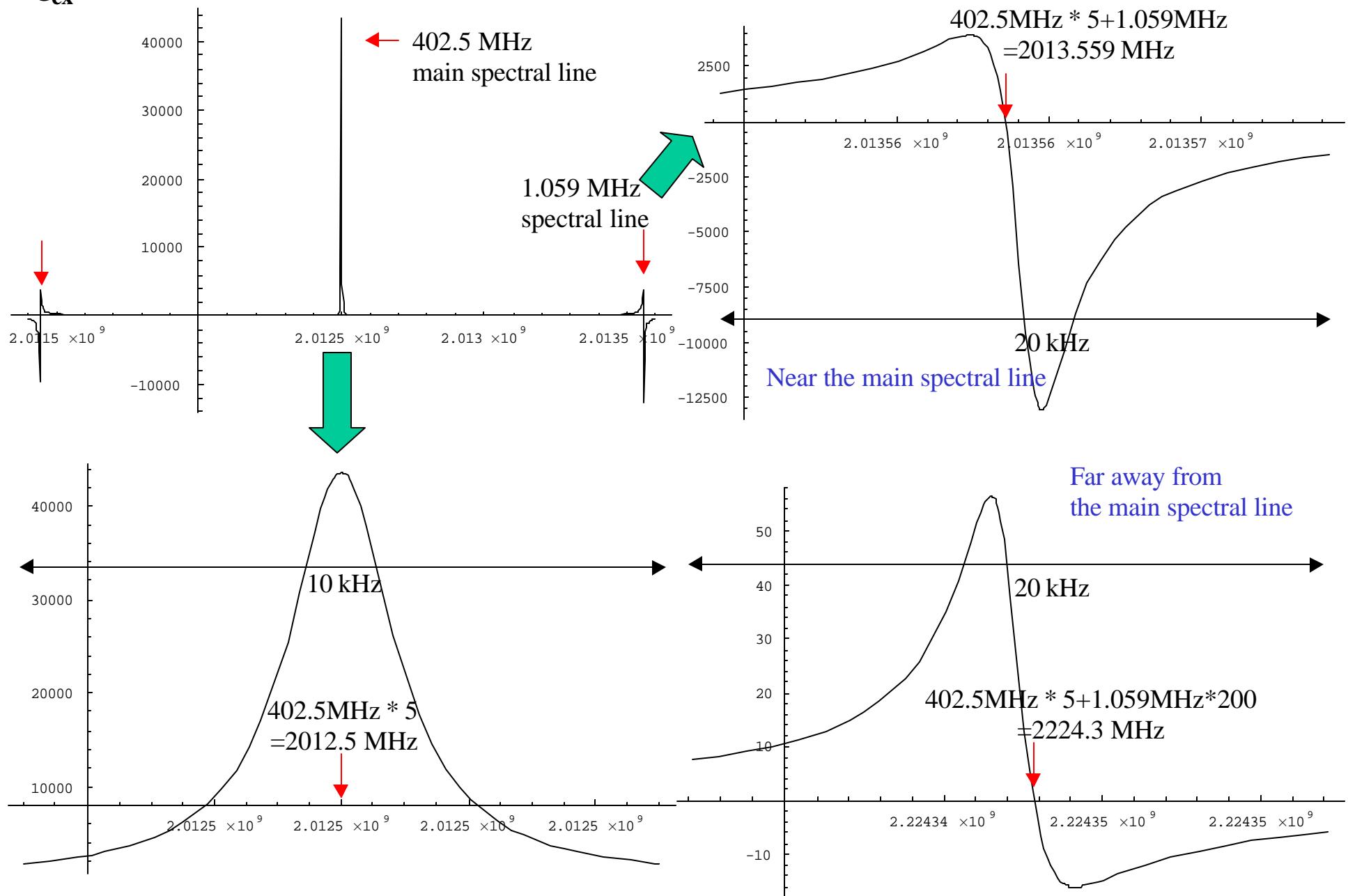
Generally Q ; order of 10^9 ,

Q_{ex} ; order of 10^6 for untrapped mode

(TTF HOM coupler; damping~30dB)

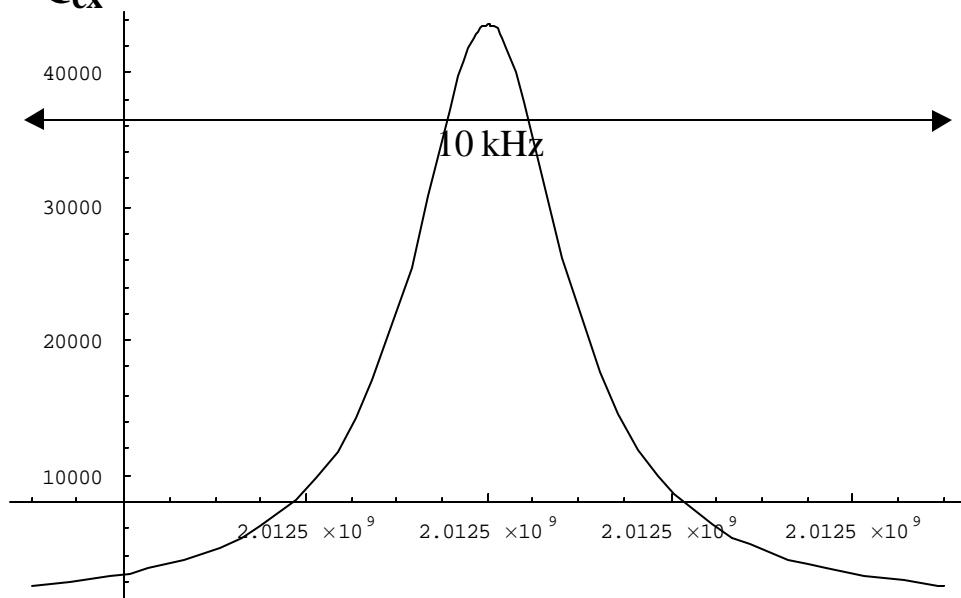
$Q_{ex}=10^6$

F; multiplication factor of spectral lines (I)

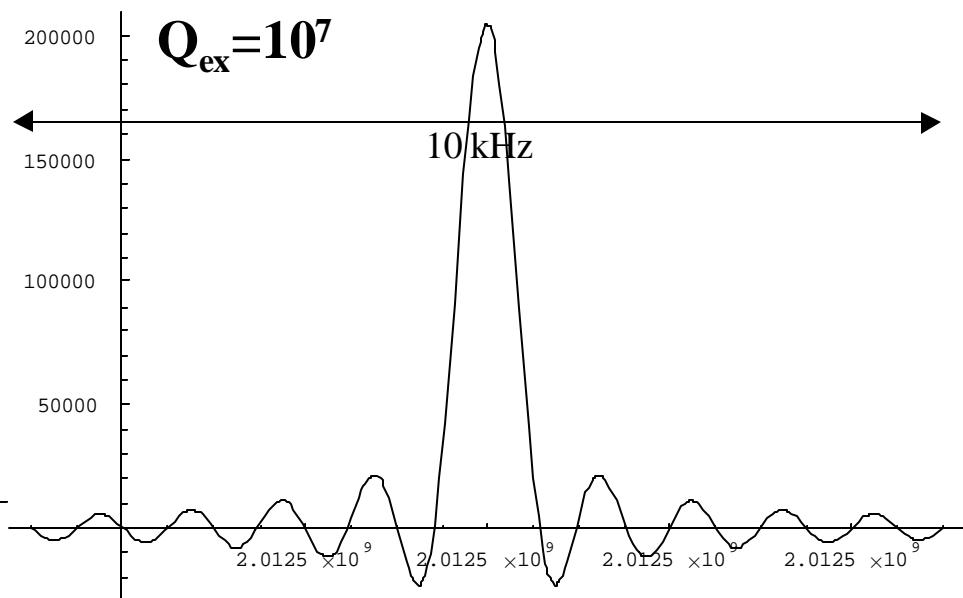


F; multiplication factor of spectral lines (II)

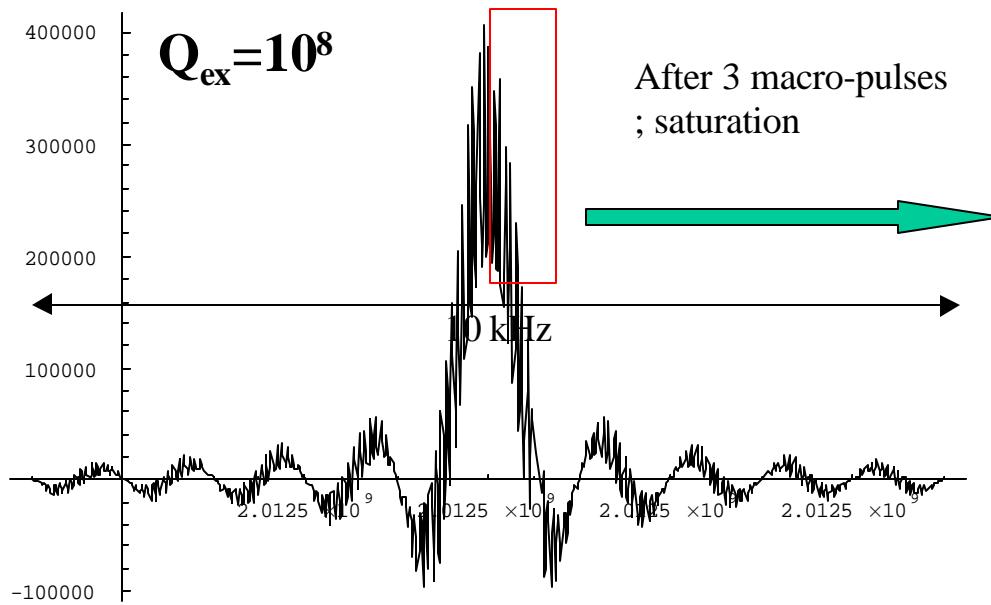
$Q_{ex}=10^6$



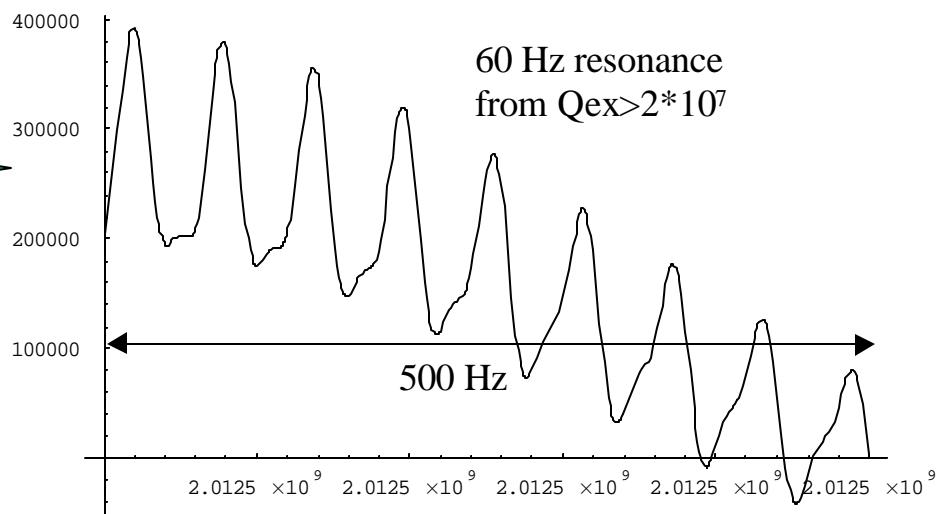
$Q_{ex}=10^7$



$Q_{ex}=10^8$



After 3 macro-pulses
; saturation



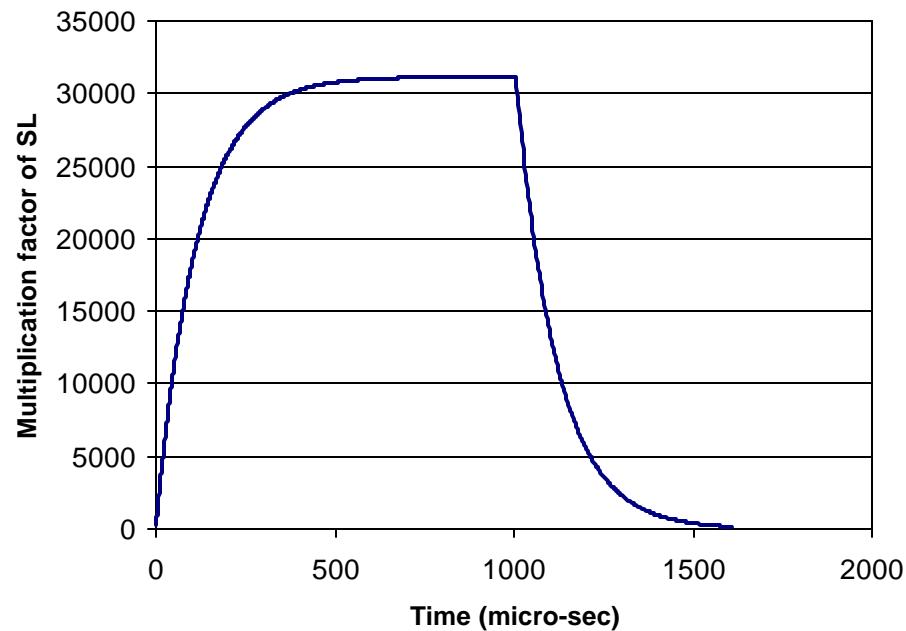
Voltage Multiplication and Decay (time dependency)

$$V_{HOMn} = \pi f_n I_0 T_b (R/Q) F$$

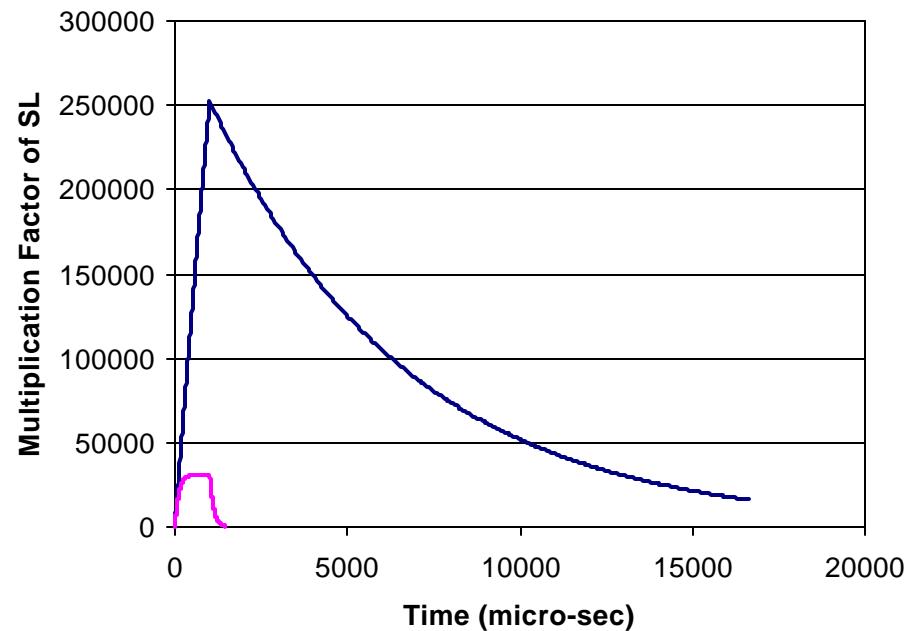
$$P_{HOMn,b} = V_{HOM,n} * I_0 \text{ (During the mid-pulse)}$$

Example; $f_n = 2.8175 \text{ GHz}$ (Main resonance frequency)

$$Q_{ex} = 10^6$$



$$Q_{ex} = 5 * 10^7$$



HOM Power

Recall HOM power equation;

$$P_{HOMn,coupler} = (\pi f_n I_0 T_b)^2 (R/Q) F^2 / Q_{ex}$$

I_0 ; beam current (52 mA during the mid pulse) → fixed

T_b ; micro bunch distance (1/402.5MHz) → fixed

R/Q ; HOM R/Q → from code result

Q ; quality factor of cavity (intrinsic) → variation is very small

**F; multiplication factor of spectral lines (from time structure)
strongly depends on HOM frequency**

f_n ; HOM frequency (frequency spread~0.3%)

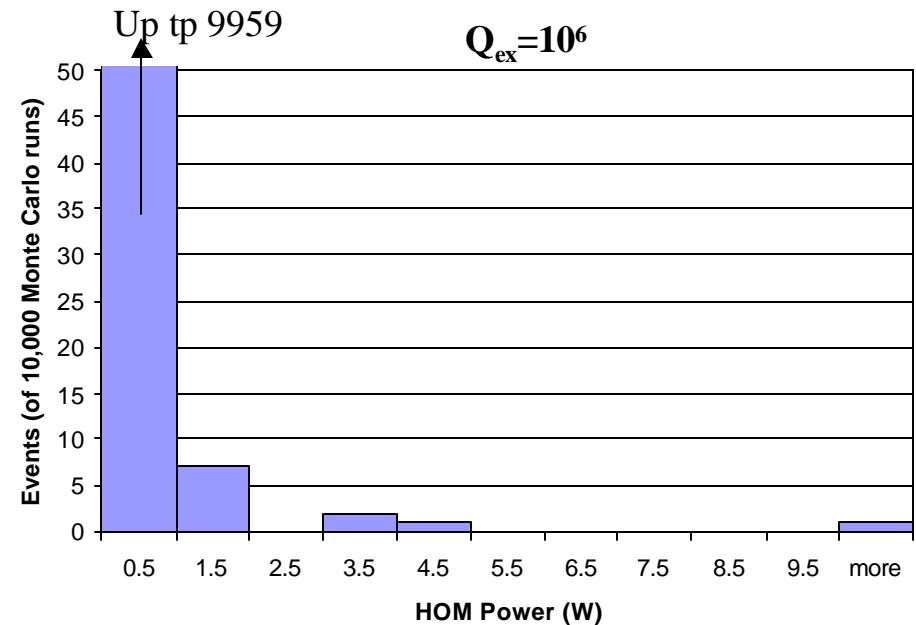
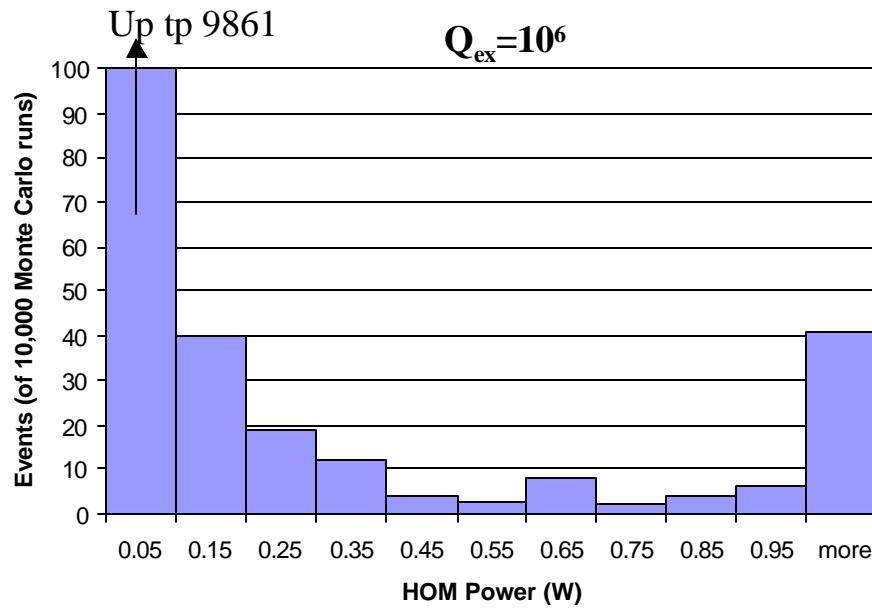
Q_{ex} ; HOM external Q (depends on stored energy in end cells)

HOM Power estimation

Stochastical results

HOM Power Estimation (example)

TM monopole mode no. 35, f=2818.8 MHz (MAFIA result), R/Q=0.4
Stored energy at both end cell combined; ~18 %



Possible maximum heat load; at 2817.5 MHz and $Q_{ex}=10^6$, Ppeak~508 W, Pavg~21W
at 2817.5 MHz and $Q_{ex}=10^7$, Ppeak~1630 W, Pavg~67W
(but probability is very small)

For other TM monopoles; in progress (results will be coming soon)