

Bunch Fourier Transform with Noise, and with Subharmonic Laser Modulation

R. Shafer 2/26/2002

The following FFT plots show the frequency domain analysis of a 400-MHz beam pulse microstructure modulated by a 100-MHz mode-locked laser, with various amounts of random micropulse amplitude jitter.

$$t := 1 .. 4095$$

$$k_t := 4 \cdot \text{round} \left(\left\langle \frac{t+3}{4} \right\rangle \right) \quad m_t := 16 \cdot \text{round} \left(\frac{t+3}{16} \right)$$

$$A_t := \delta(t+3, k_t) \quad B_t := \delta(t+3, m_t)$$

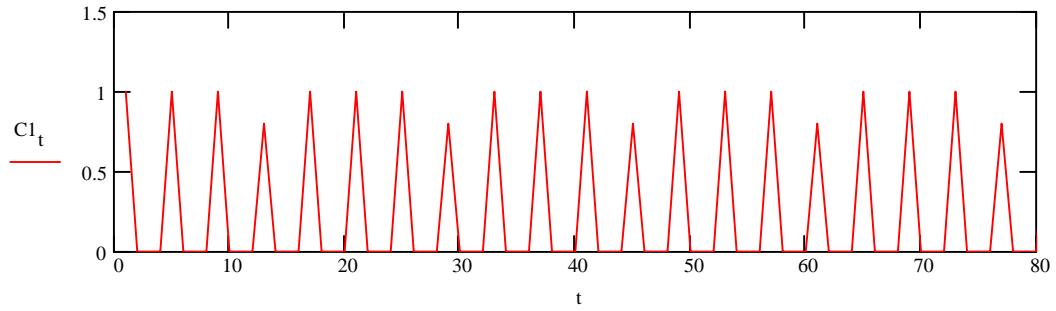
$$C1_t := (1 + 0.0001 \cdot (\text{rnd}(1) - 0.5)) \cdot (A_t - 0.2 \cdot B_t) \quad \text{length}(C1) = 4.096 \cdot 10^3$$

$$C2_t := (1 + 0.0001 \cdot (\text{rnd}(1) - 0.5)) \cdot (A_t - 0.01 \cdot B_t)$$

$$C3_t := (1 + 0.001 \cdot (\text{rnd}(1) - 0.5)) \cdot (A_t - 0.001 \cdot B_t)$$

$$C4_t := (1 + 0.01 \cdot (\text{rnd}(1) - 0.5)) \cdot (A_t - 0.0001 \cdot B_t)$$

Time structure of 400-MHz micropulses, showing 20% laser modulation at 100 MHz



$$N := 4096$$

$$j := 0 .. \frac{N}{2}$$

===== Fast Fourier Transforms =====

$$F1 := \text{fft}(C1)$$

FFT of C1

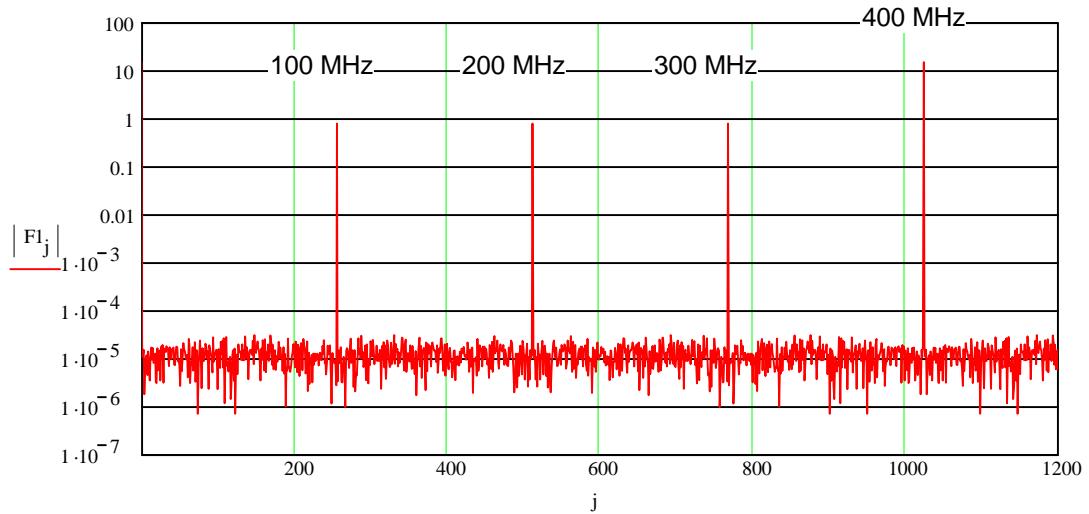
$$\text{length}(F1) = 2.049 \cdot 10^3$$

$$F2 := \text{fft}(C2)$$

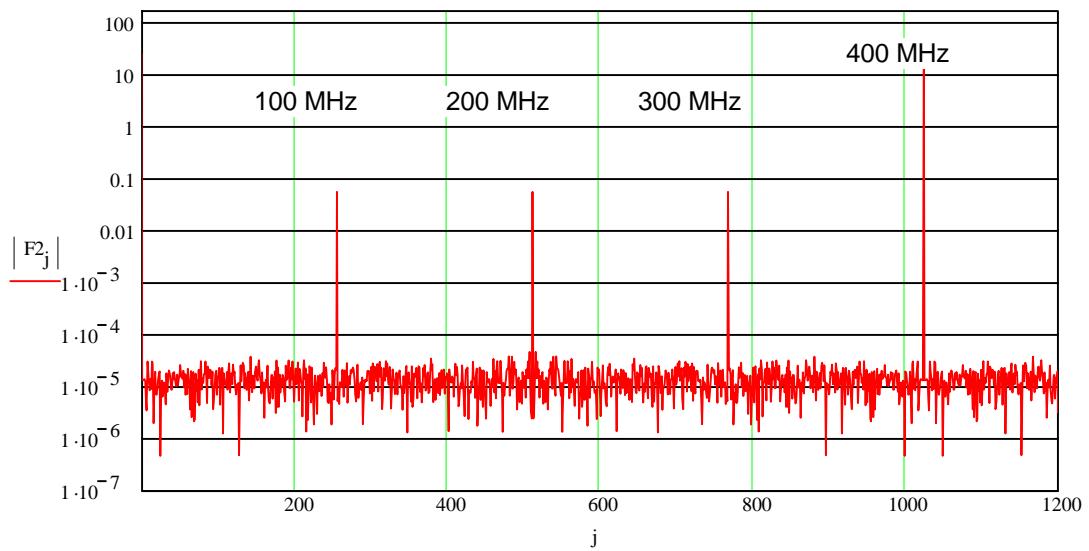
$$F3 := \text{fft}(C3)$$

$$F4 := \text{fft}(C4)$$

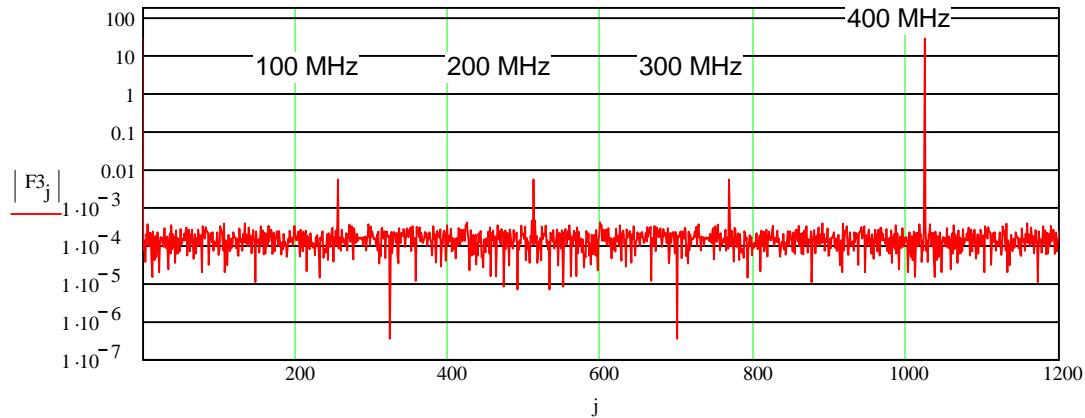
20% laser modulation, 0.01% random noise



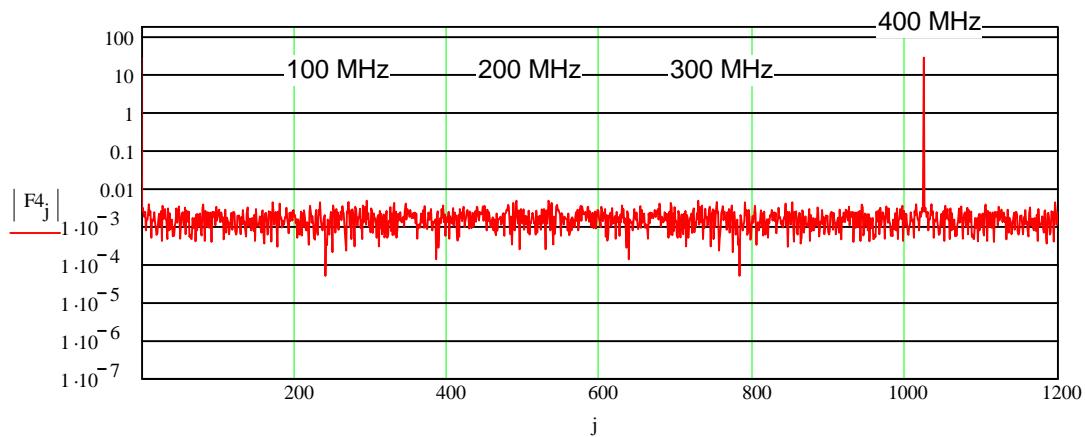
1% laser modulation, 0.01% random noise



0.1% laser modulation, 0.1% random noise



0.01% laser modulation, 1% random noise



Where's the signal?