

ACNS

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Free Lunch Theorem in Pulsed Source Instrument Optimization

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HMI & LANL

Flux on sample

Continuous sources:

$$\varphi = \eta \Phi \delta\Omega \delta\lambda$$

Performance: Flux / (Wavelength) Resolution Ratio (FRR)

$$\varphi / \delta\lambda = \eta \Phi \delta\Omega = \text{const. for given } \lambda$$

→ *Flux and resolution directly (inversely) related*

No free lunch!

Pulsed sources: elastic scattering & inverted geometry spectroscopy

$$\varphi = \int_{\lambda_{\min}}^{\lambda_{\max}} \eta \Phi \delta\Omega d\lambda$$

→ **No direct relation between flux and resolution !!!**

$$\Delta\lambda = \lambda_{\max} - \lambda_{\min} = c T/L$$

$$c = 3.96 \text{ \AA}\cdot\text{m/ms}$$

T = source pulse repetition time

$$\delta\lambda = c dt/L$$

dt = source pulse length, f = dt / T = duty factor

L = source-detector (sample) distance

L is a crucial design parameter, FRR is L dependent

but in direct view $\varphi \propto \delta\Omega \propto 1/L^2$. Constrain for L!

Old instrument design paradigm:

shortest possible distance to mitigate $1/L^2$ (or guide losses)

→ shortest pulse to keep resolution

→ lowest source brightness

Advances in neutron beam delivery

Supermirror neutron optics:

$\delta\Omega$ of direct view (or more) can be delivered with small beam losses for both thermal and cold neutrons to any distance $10 \text{ m} < L < 1 \text{ km}$

New instrument design paradigm:

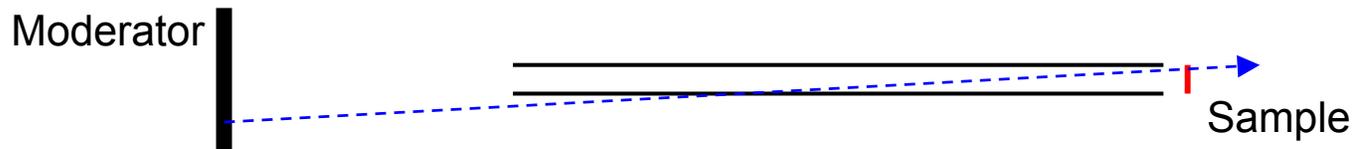
$\eta\delta\Omega$ is independent of L , thus

L becomes a free instrument design parameter

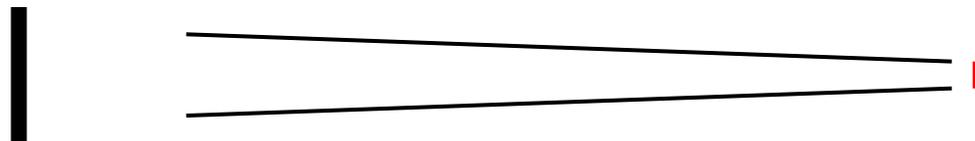
Neutron beam delivery for short wavelength neutrons
over shortest feasible distances to sample (~12 m):
direct view of moderators implies very small solid angle
(0.5°x 0.5° vs. up to 2°x 5° at reactor sources)

Supermirror neutron optics offers improvement

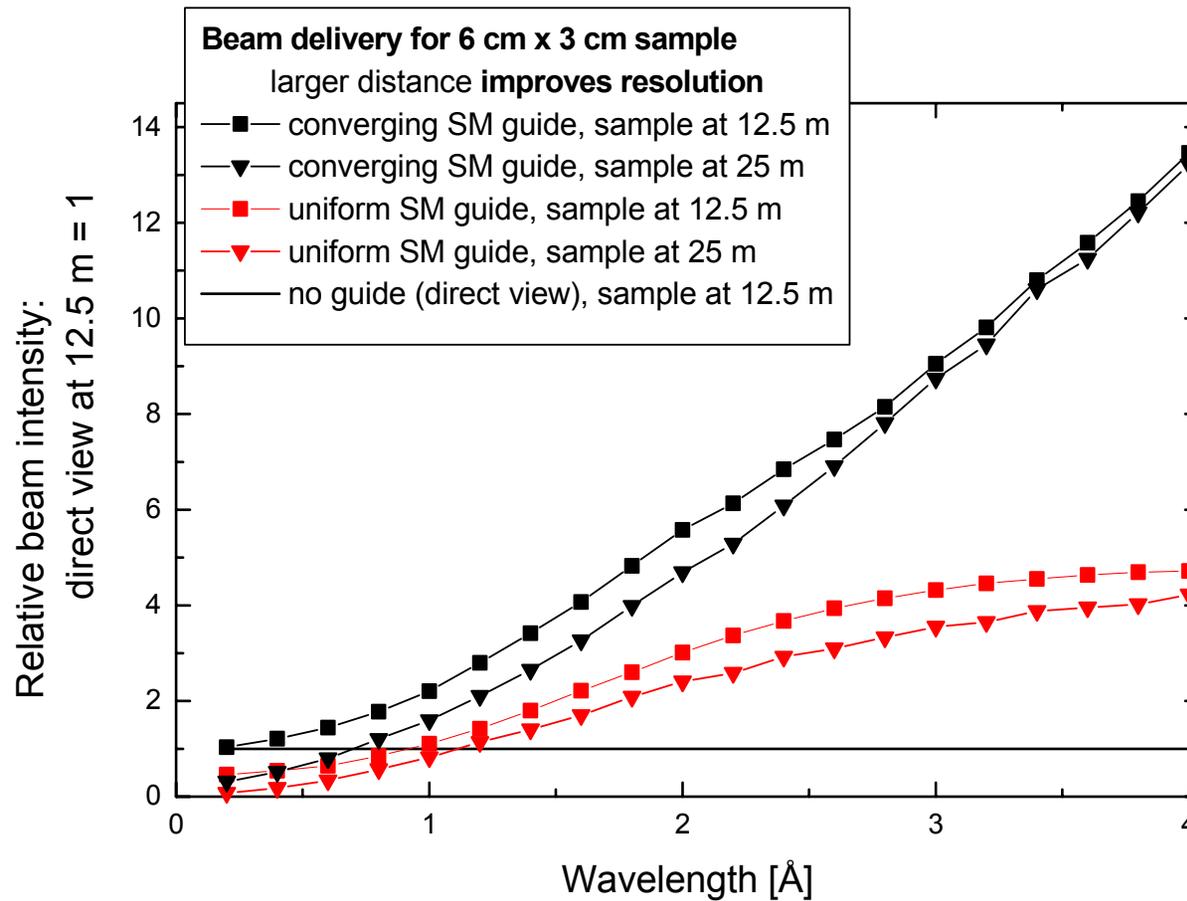
Conventional uniform guide: shadows direct view



Converging neutron guide: combines reflection and direct view

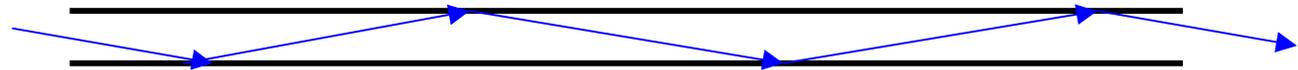


Supermirror optics: enhanced beam delivery for all distances
for $\lambda > 0.8 \text{ \AA}$

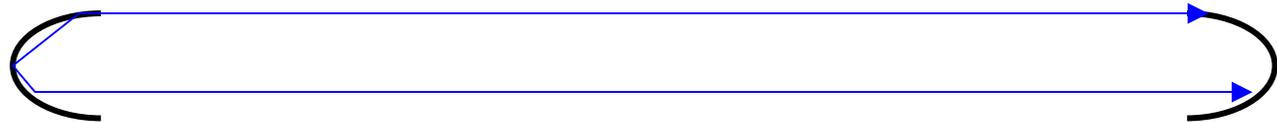


Neutron beam delivery over large distances:
neutron guides

But reflection losses are still substantial:



Principle of **ballistic** guide: reduce the number of reflections:



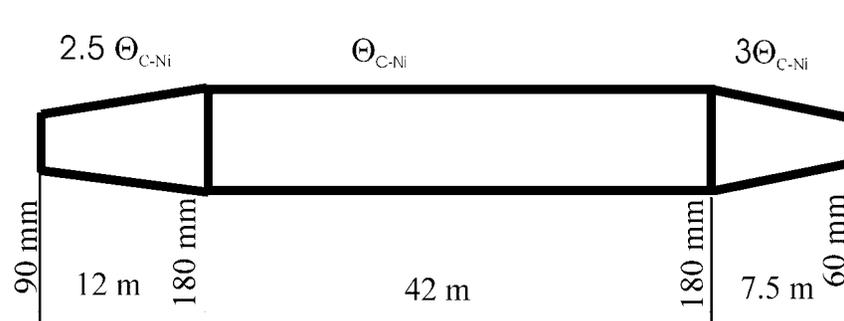
Prototype ballistic guide in the making (LANSCE)

Average number of reflections at 10Å:

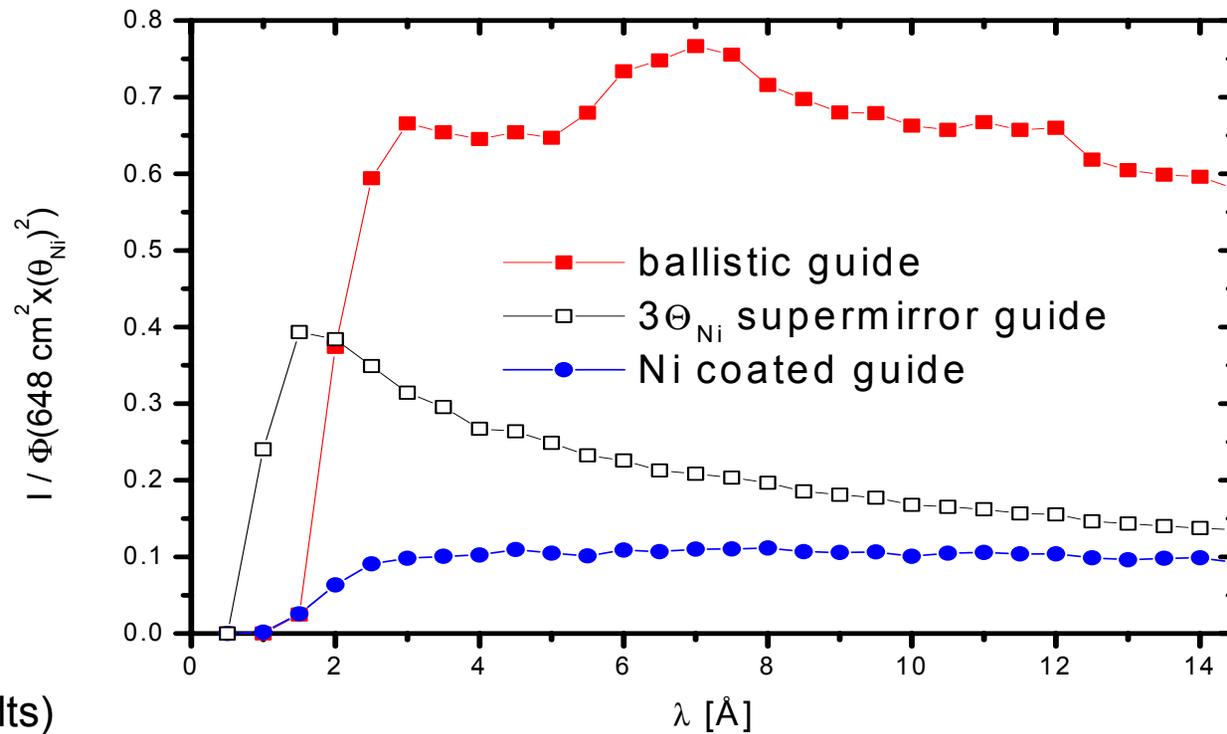
SM guide 70

Ni guide 25

Ballistic guide 10



Largely enhanced beam delivery over large distance (> 60 m)



(Simulation results)

Flux on sample

Pulsed sources: elastic scattering and inverted geometry spectroscopy

$$\varphi = \int_{\lambda_{\min}}^{\lambda_{\max}} \eta \Phi \delta\Omega d\lambda$$

→ **No direct relation between flux and resolution**

$$\Delta\lambda = \lambda_{\max} - \lambda_{\min} = c T/L$$

$$c = 3.96 \text{ \AA}\cdot\text{m/ms}$$

T = source pulse repetition time

$$\delta\lambda = c dt/L$$

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L = source-detector (sample) distance

If L is variable at constant $\delta\Omega$:

$$L \rightarrow \infty : \varphi = \eta \Phi \delta\Omega \Delta\lambda = \eta \Phi \delta\Omega \delta\lambda / f$$

narrow band limit, FRR is independent of L (like CW)

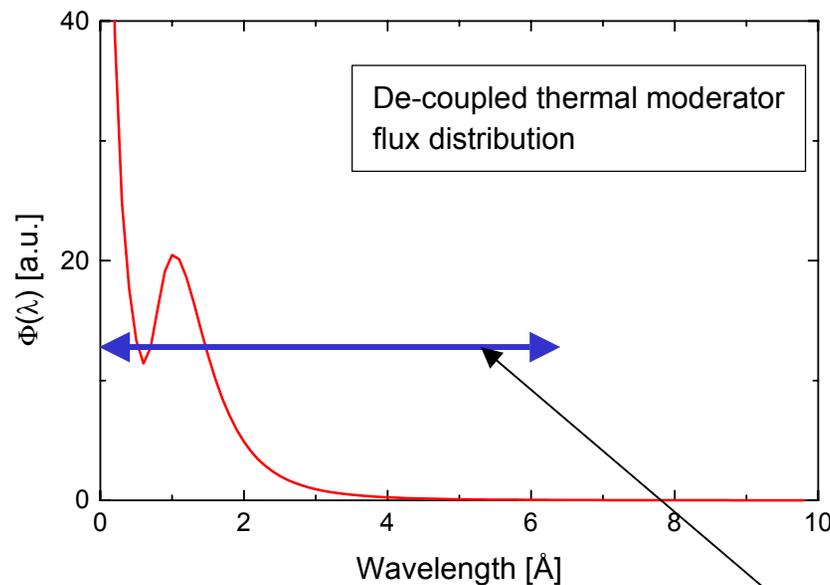
$$L \rightarrow 0 : \varphi = \int \eta \Phi \delta\Omega d\lambda = \text{const}$$

broad band limit, **FRR \propto L** = **Free lunch!**

Free lunch theorem for pulsed source instruments:

Non-uniform flux (or information contents) distribution makes FRR steadily increase with increasing L: on a given beam the **resolution increases without loss of intensity.**

Small print: $\lambda > 0.8 \text{ \AA}$, long guides and wavelength band definition choppers are needed, residual losses introduce an optimal length,

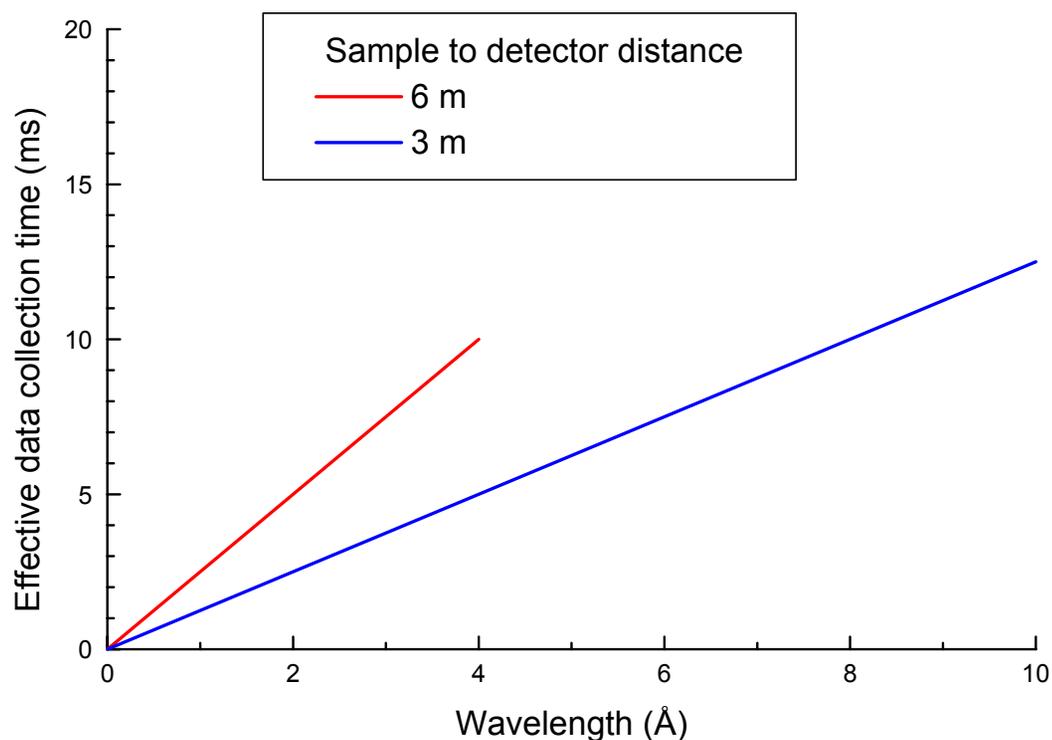


Optimal length varies case by case: e.g. 50 Hz source frequency, $\sim 40 - 50 \text{ m}$ for thermal neutron machines, 600 m for sub- μeV back-scattering

Wavelength band at $L=12 \text{ m}$ and 50 Hz

Direct geometry TOF spectroscopy:

Flux relations different, but plenty of room for improvements:
low source frequency leads to overwhelming data collection
dead times in TOF spectroscopy



Inelastic scattering:

*analysis of velocity after scattering on sample only
requires 2 - 10 ms: ideal pulse repetition 100 - 500 Hz*

Repetition Rate Multiplication (RRM): several pulses on sample from each source pulse (prototype in the making at LANSCE)

Example:

at $\lambda = 1 \text{ \AA}$

$\lambda_{i+1} - \lambda_i \sim 0.1 \text{ \AA}$

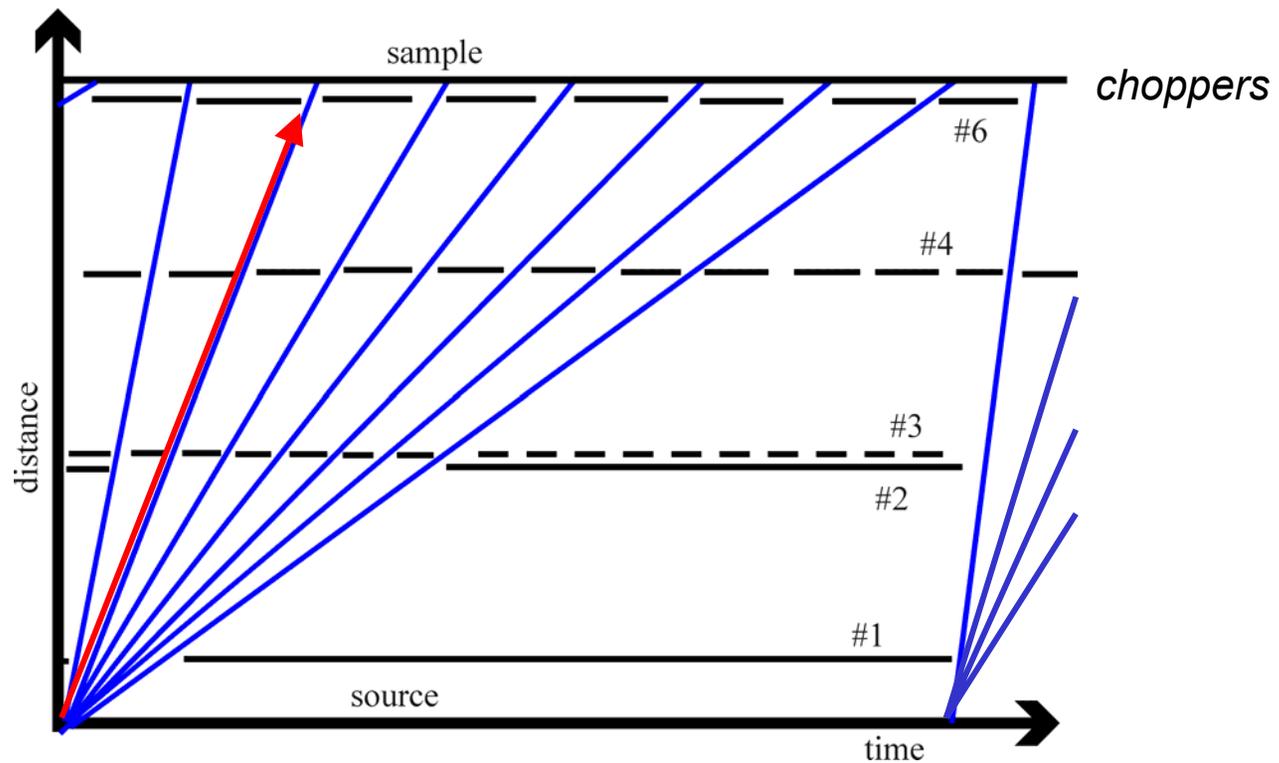
for $D_{ms} = 50 \text{ m}$

and $D_{sd} = 3 \text{ m}$

at least

4 - 8 pulses

productive



Chopper spectrometers:

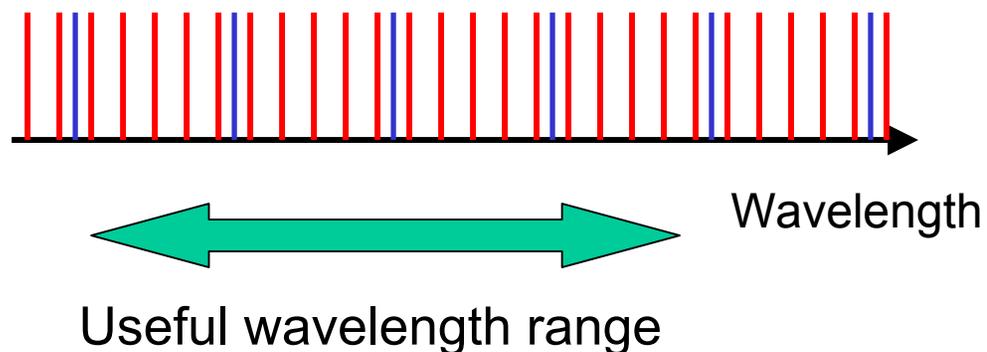
intensity at constant chopper pulse length: $\propto 1/L$

number of pulses per unit wavelength with RRM: $\propto L$

→ flux on sample independent of L (i.e. same as for diffraction and inverted geometry) if RRM is used

Example:

RRM wavelength sequences for $L_{\text{red}} = 4 \times L_{\text{blue}}$

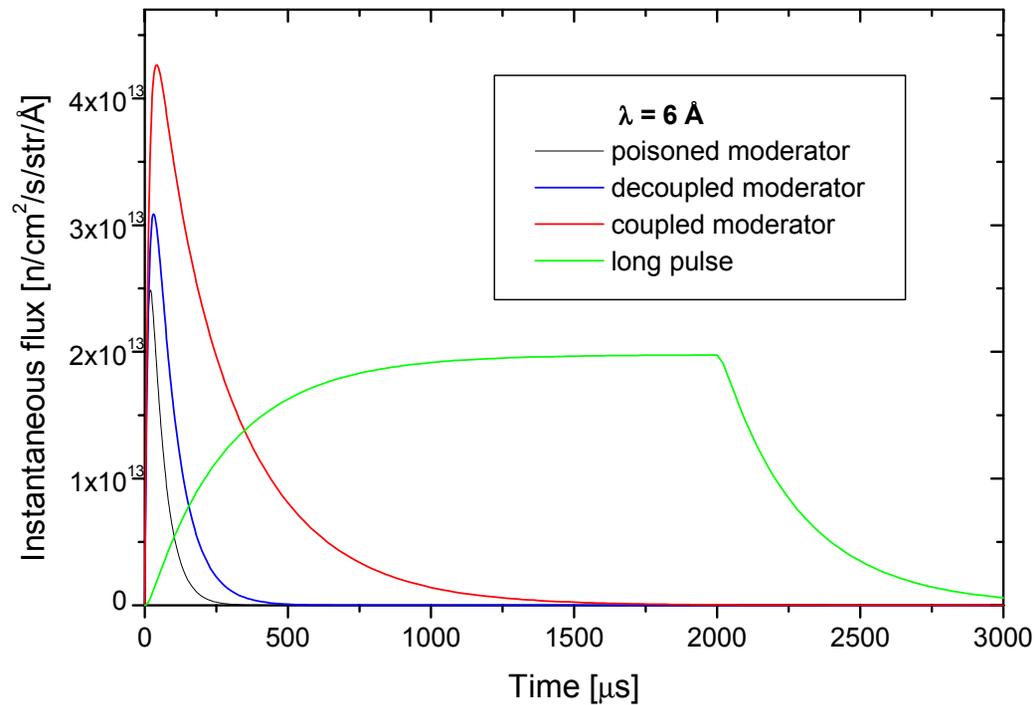


New instrument design paradigm (except eV range):

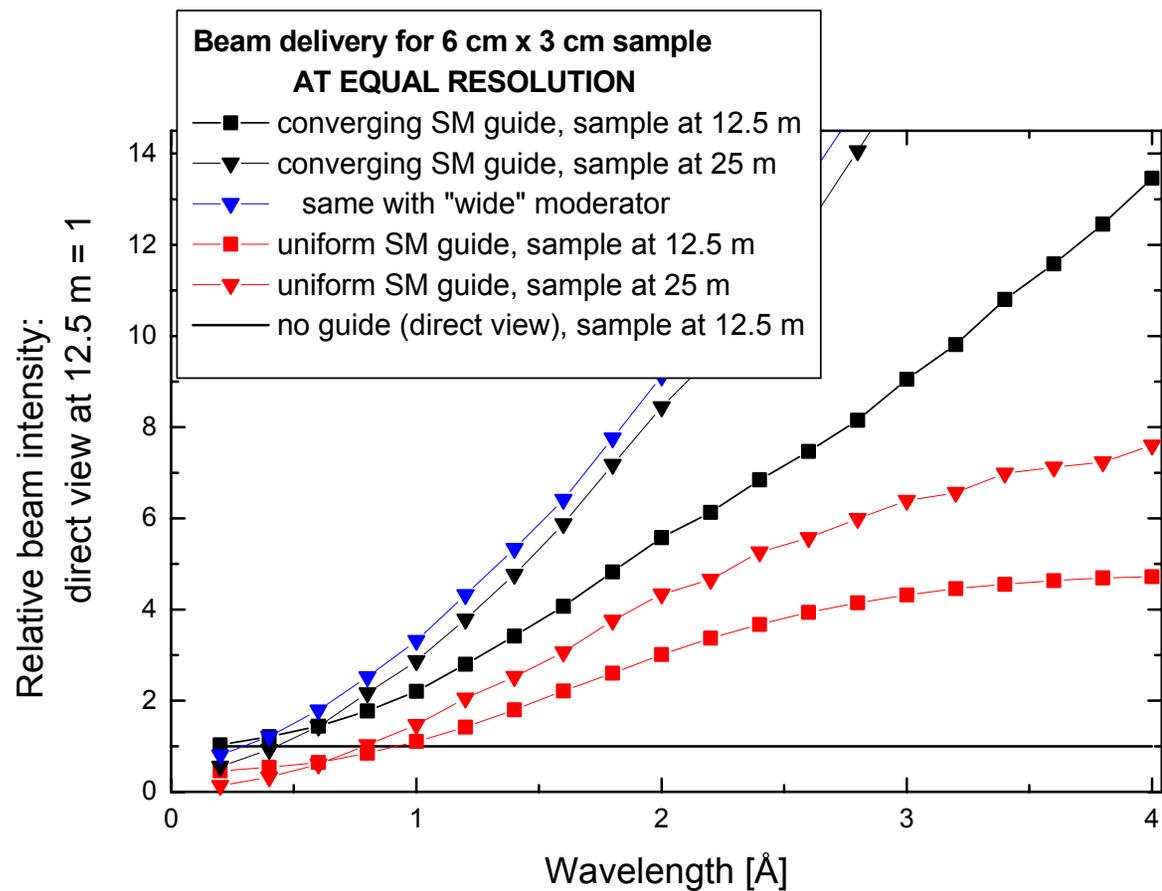
longest possible distance to achieve resolution with the most intense (i.e. longest) pulses

→ highest source brightness

To maximize intensity at constant resolutions: guides efficient for $\lambda > 0.5 \text{ \AA}$



Supermirror guides can make the **enhanced intensity** of less poisoned moderators available **without loss of resolution** for $\lambda \geq 0.5 \text{ \AA}$



Summary:

Advanced neutron guides efficient for wavelengths $> 0.5 \text{ \AA}$

No $1/L^2$ penalty for large source-detector (sample) distances

Long instruments with sharply defined wavelength band eliminate much of the dead /low efficiency data collection time

Free lunch: turning (some of the) dead time into prime data collection time:

for enhanced resolution without intensity loss: longer instrument

for enhanced intensity without resolution loss: longer source pulses + longer instruments

