

Bragg Glass Superconductivity



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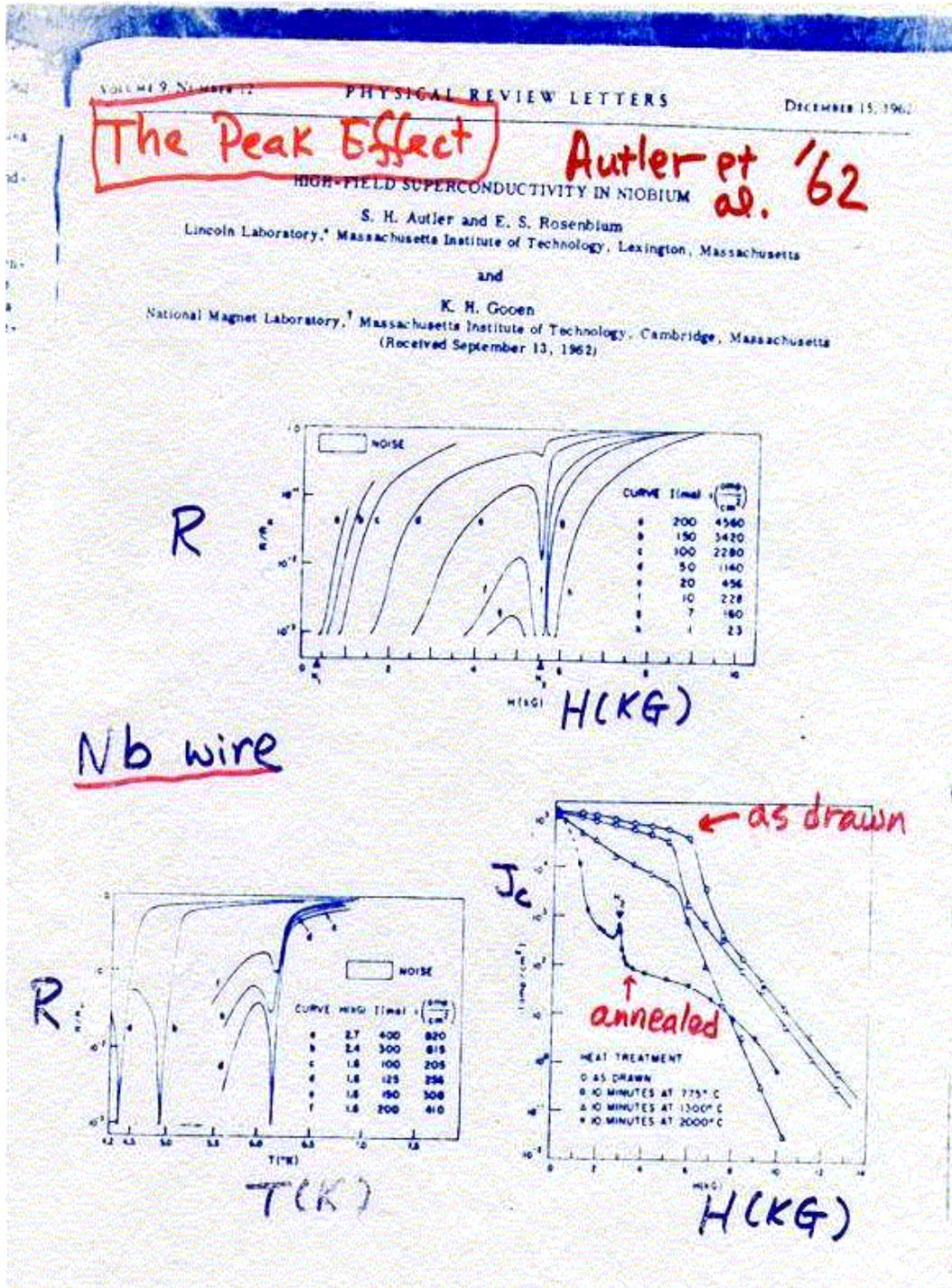
Funding:

NSF-DMR, Sloan

Outline:

- The peak effect problem (1962-2002):
observed in most weak-pinning type-II superconductors
- Larkin-Ovchinnikov collective pinning model (1970-1979):
loss of long-range-order (LRO)
peak effect = anomalous softening of vortex lattice
- Can there be a real solid-liquid phase transition in vortex matter?
Bragg glass model (1990-1995): survival of topological LRO
A true solid-liquid transition should be possible!
- Peak effect = Bragg glass melting transition?
Brown-NIST experiment: *in-situ* neutron scattering

X.S. Ling, S.R. Park, B.A. McClain, S.M. Choi, D.C. Dender, J.W. Lynn, PRL **86**, 712 (2001).
S.R. Park, I. Dimitrov, S.M. Choi, D.C. Dender, J.W. Lynn, X.S. Ling (to be submitted).



The Peak Effect Problem:

Peak effect in high- T_c YBCO:

Ling, Budnick (1991)

D'Anna (1993)

Kwok, Crabtree (1994)

Shi, Ling (1999)

Peak effect in 2H-NbSe₂ and other low- T_c systems (1993-):

Bhattacharya, Higgins

Andrei, Xiao

Kes

Ling, Berger

Gammel, Bishop,

Zeldov

Ling, Park, Lynn (2001)

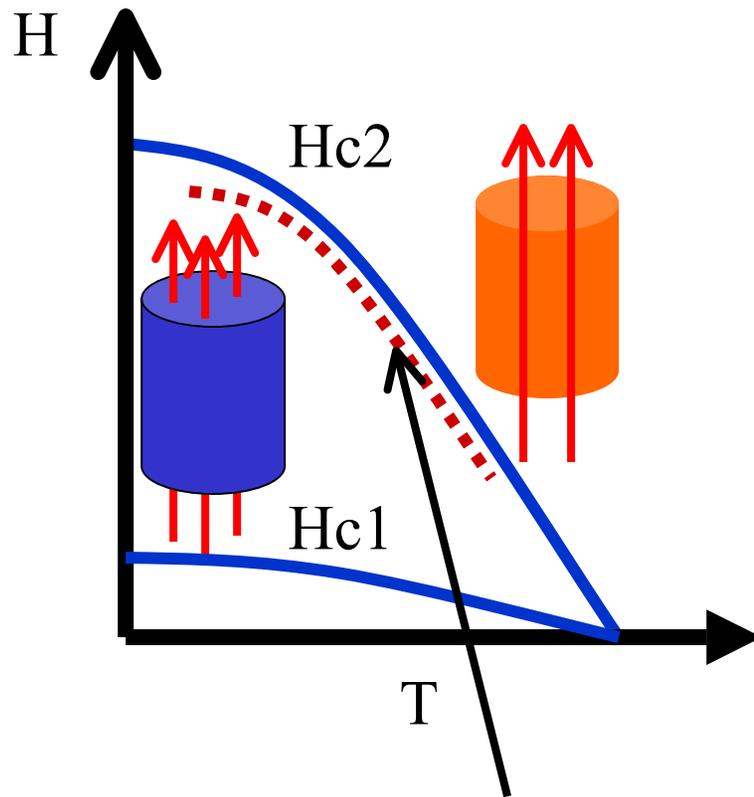
2nd-peak effect in BSCCO may be related to the peak effect:

Konczykowski

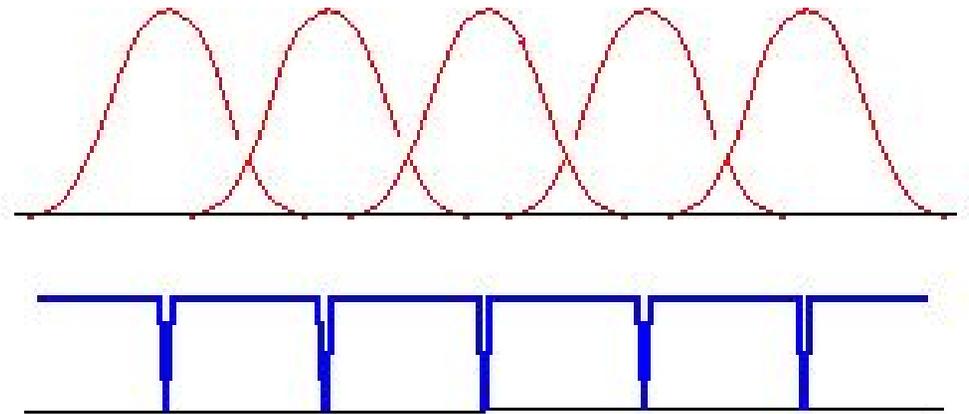
Tamegai

Zeldov

Type-II Superconductors

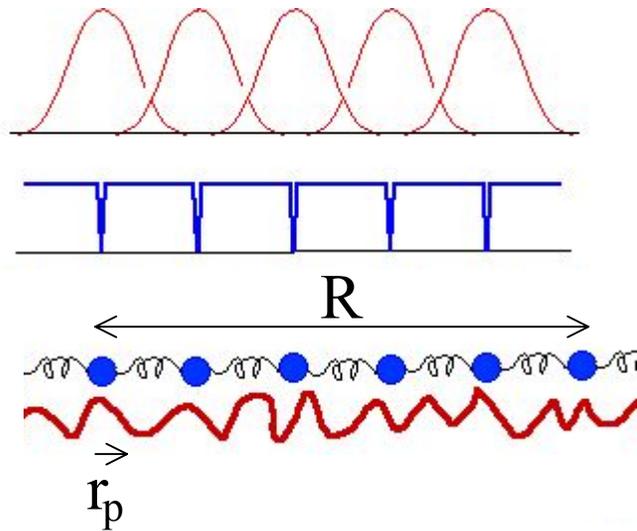


Abrikosov lattice



location of the peak effect in low- T_c systems

Random pinning destroys long-range order!

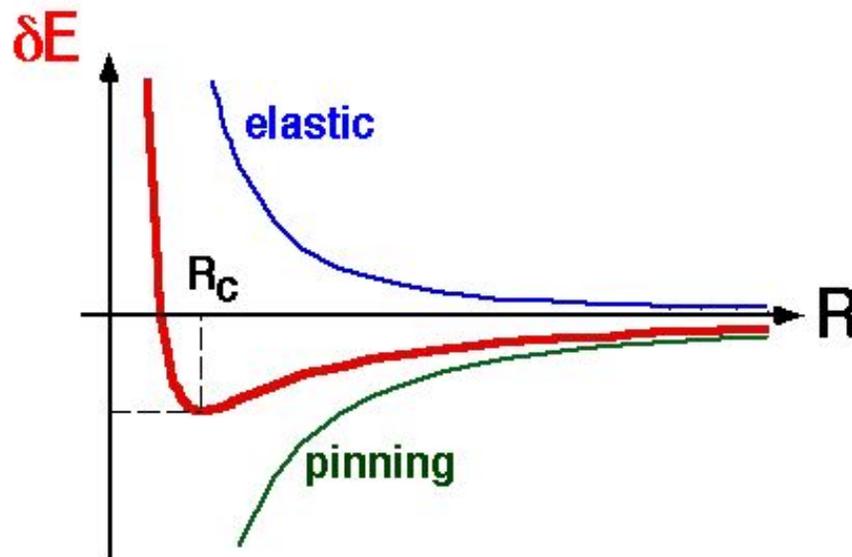


A.I. Larkin (1970)

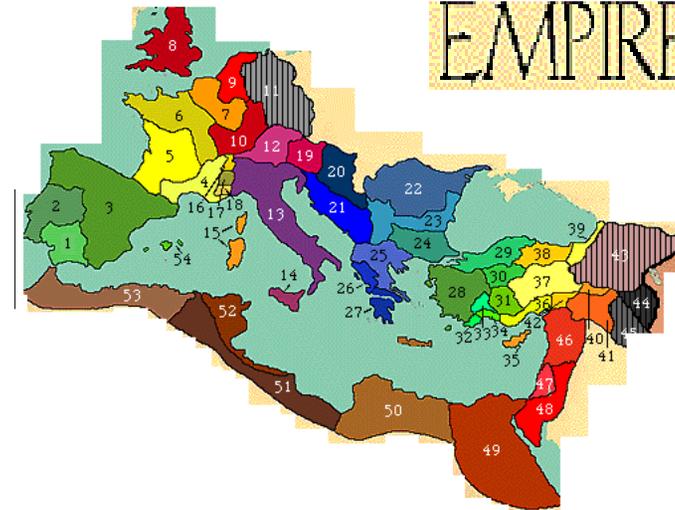
Y. Imry, S.-k. Ma (1975)

P.A. Lee, T.M. Rice (1980)

$$\delta E = C_{66} \left(\frac{r_p}{R} \right)^2 + C_{44} \left(\frac{r_p}{L} \right)^2 - f r_p \left(\frac{n}{R^2 L} \right)^{1/2}$$

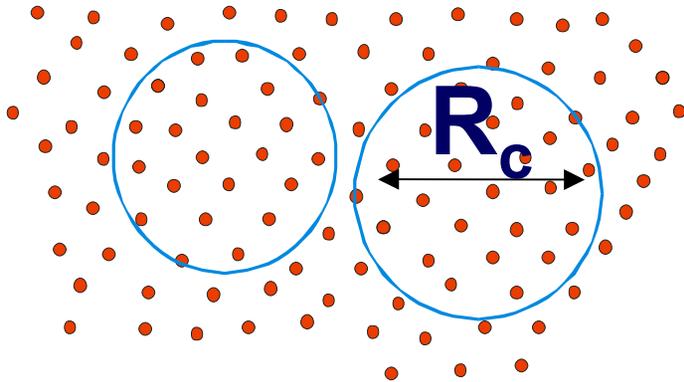


ROMAN
EMPIRE



Collective Pinning Model

A.I. Larkin, Yu. Ovchinnikov (1979)

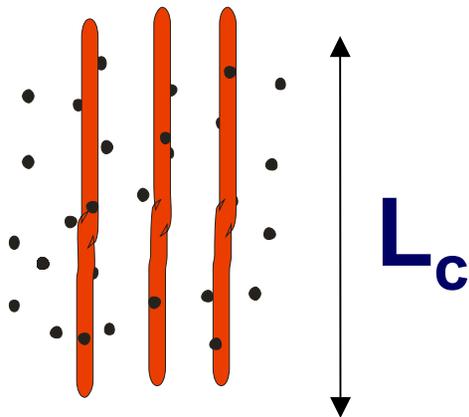


$$F_p = \frac{\sqrt{N}f}{V_c} = \sqrt{\frac{nf^2}{V_c}} = J_c B = \frac{n^2 f^4}{C_{66}^2 C_{44} r_p^3} \quad \text{3D}$$

$$R_c \equiv \frac{C_{66}^{3/2} C_{44}^{1/2} r_p^2}{n f^2}$$

$$\frac{L_c}{R_c} = \sqrt{\frac{C_{44}}{C_{66}}}$$

$$= \frac{n f^2}{C_{66} r_p^d} \quad \text{2D}$$

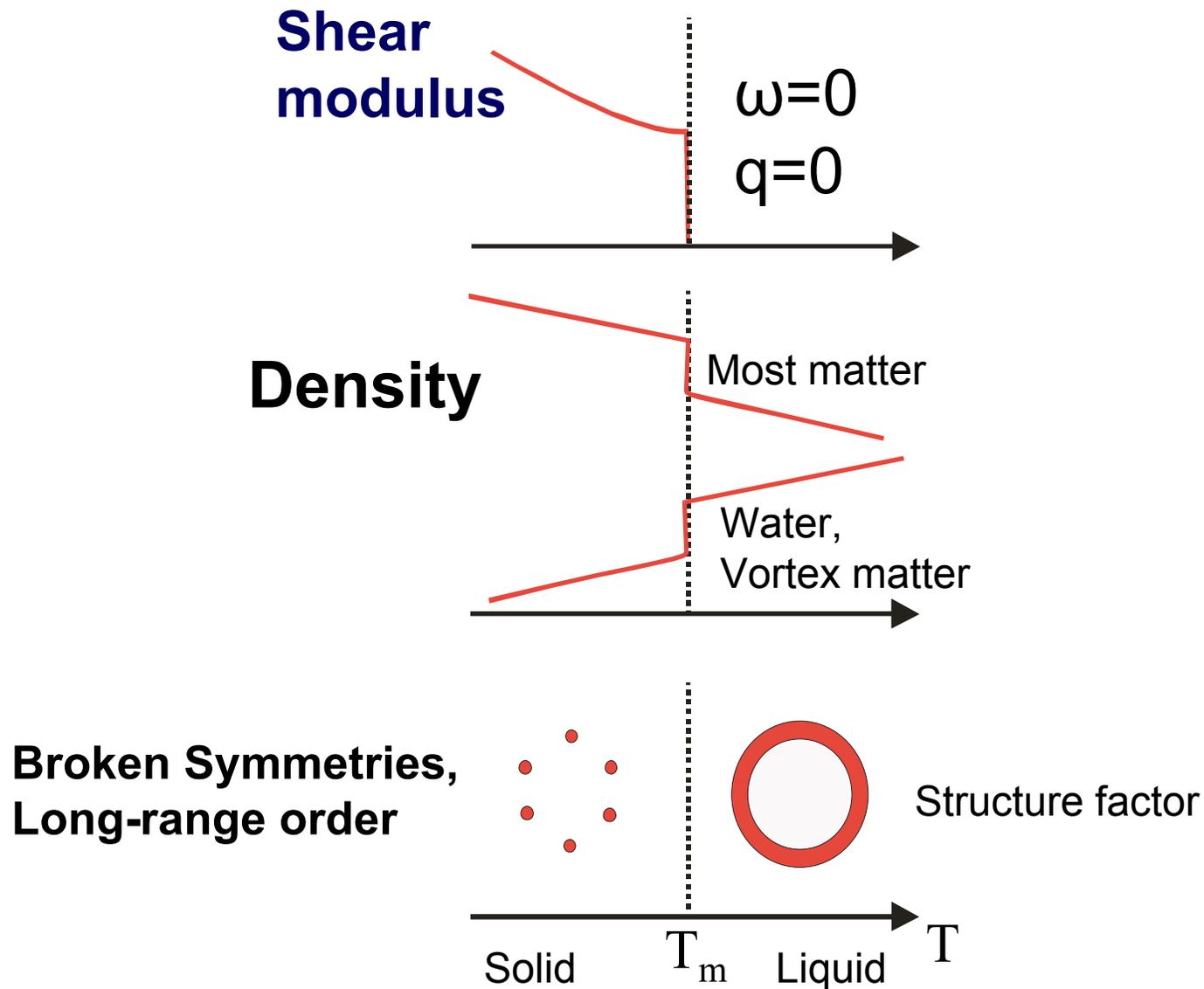


In the Larkin model, the peak effect is caused by a sudden softening of the vortex lattice.

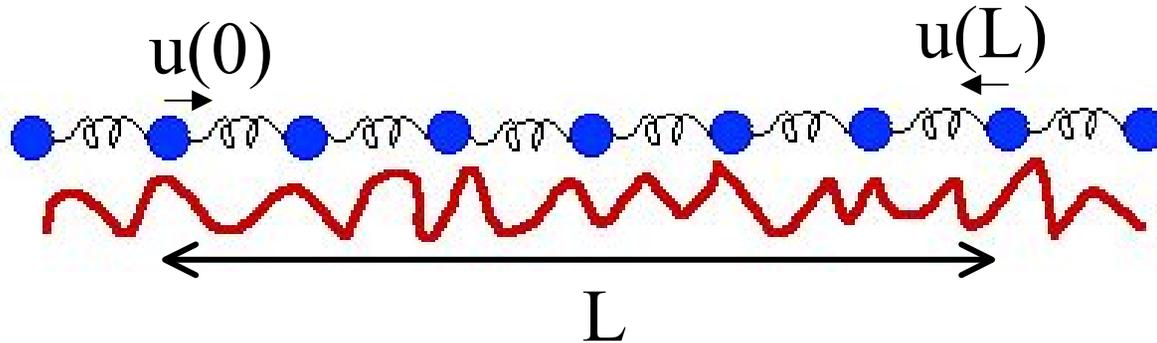
Is it a phase transition?

Signatures of conventional solid-liquid transitions:

1st order phase transitions



weak random pinning systems



$$\overline{\langle [u(L) - u(0)]^2 \rangle} = A \log L$$

**Quasi-long-range-order can survive in
3D weak pinning systems!**

T. Nattermann (1992)
T. Giamarchi,
P. le Doussal (1995)

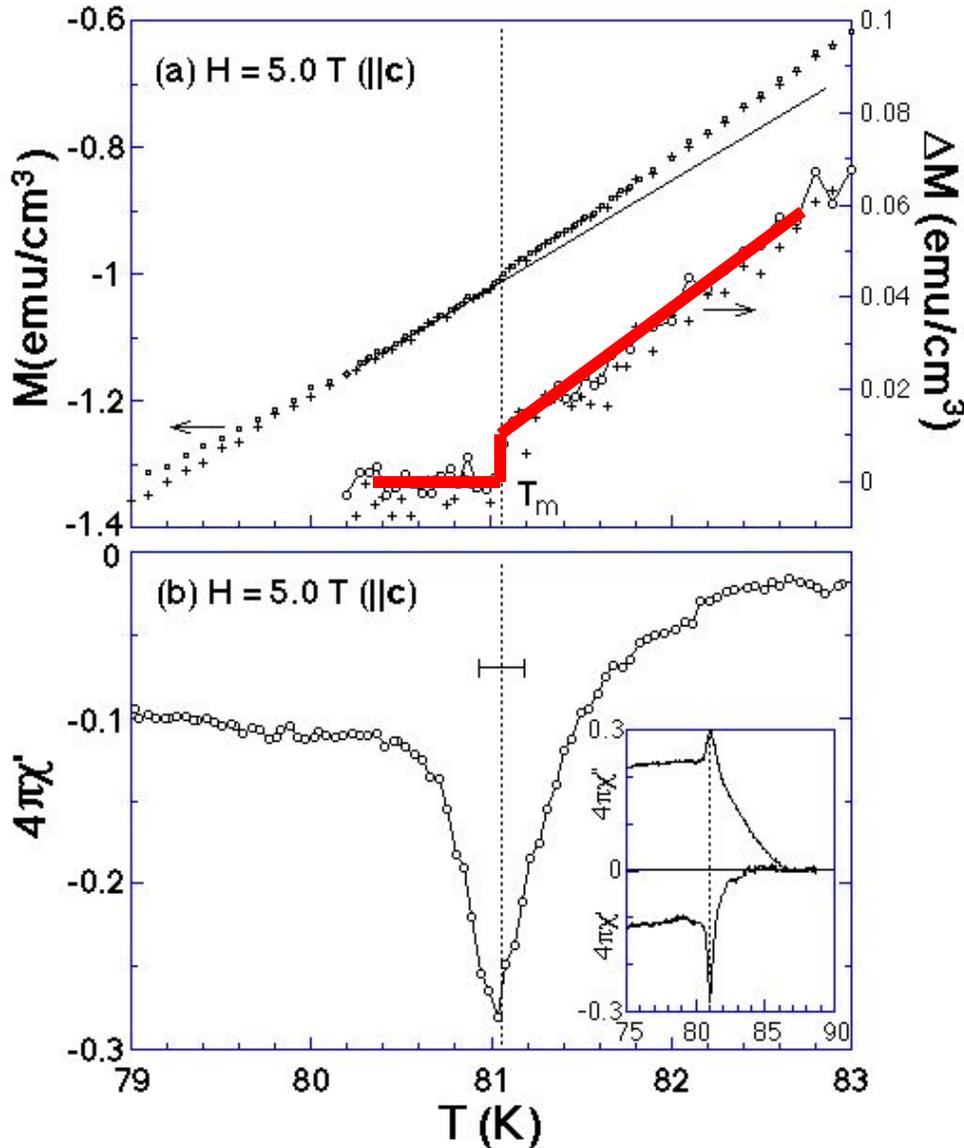
It's a Bragg glass!

A real solid-liquid transition is possible.



First Hint from YBaCuO:

coincidence of peak effect and magnetization jump



T. Ishida (1997)

J. Shi, X.S. Ling, R. Liang, D. Bonn, W. Hardy (1999).

Also in BSCCO:

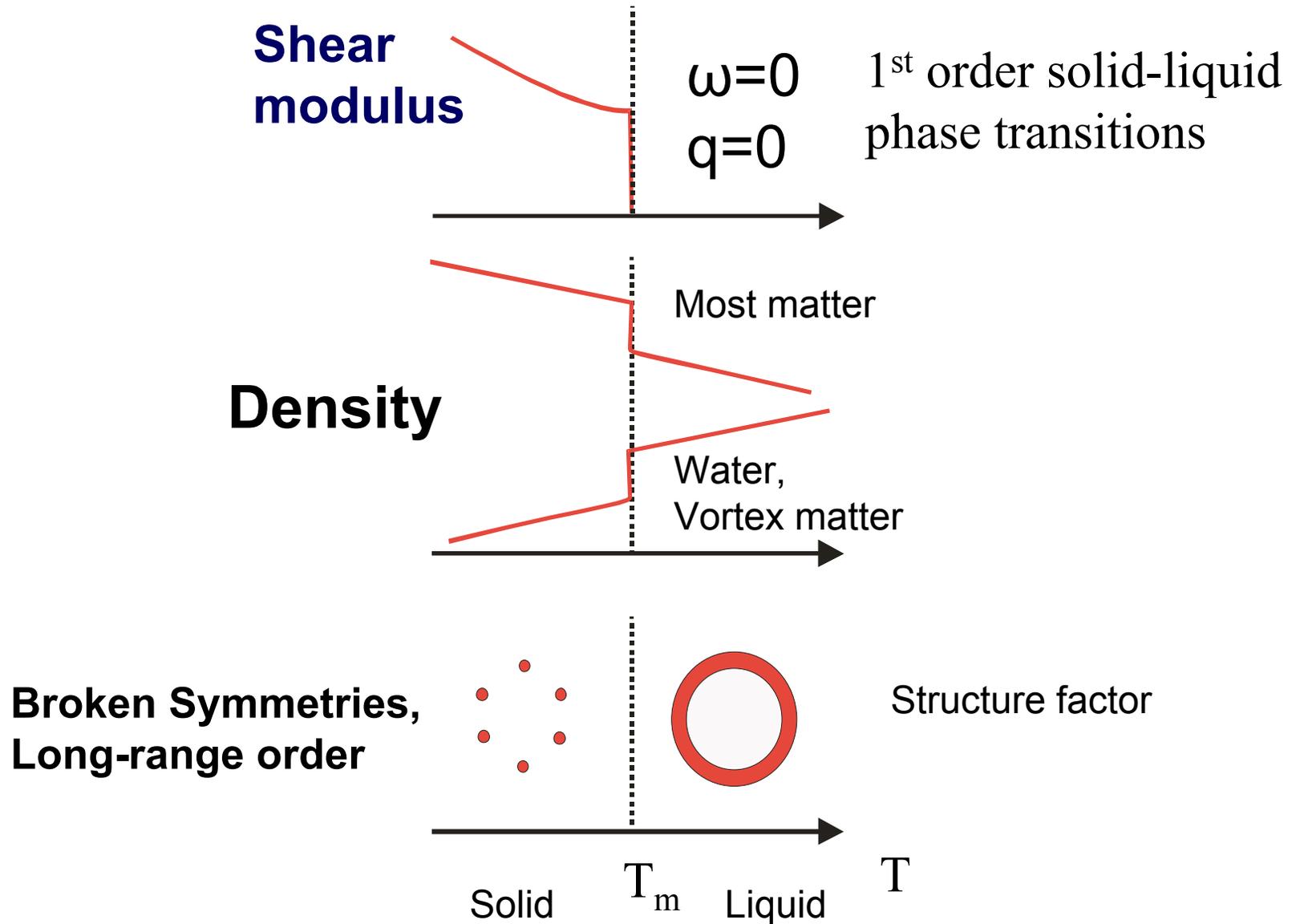
N. Avraham, E. Zeldov et al. (2002)

$$\mathbf{B} = \mathbf{H} + 4\pi\mathbf{M}$$

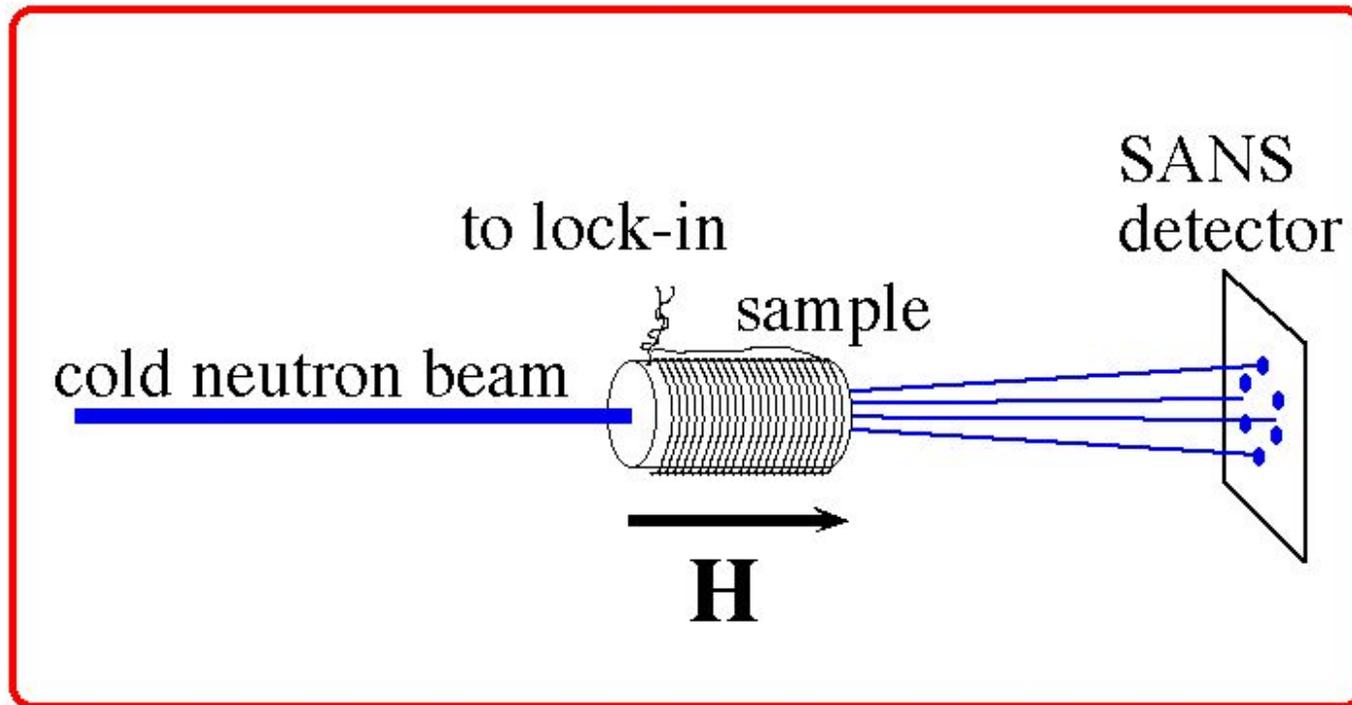
$$\mathbf{B} = \mathbf{n} \phi_0$$

↑
Vortex
density

Now, we still need structural evidence



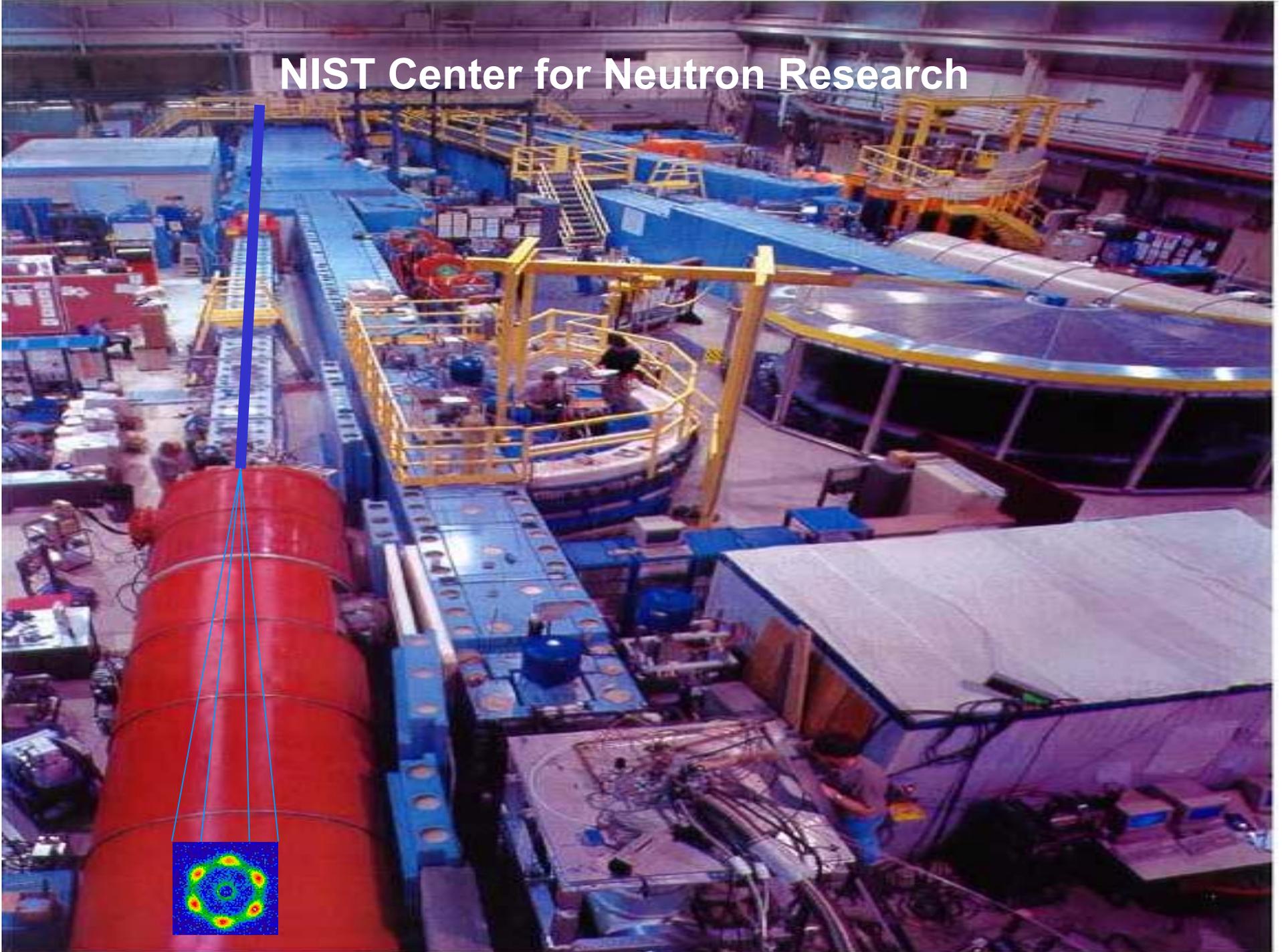
Experimental Configuration



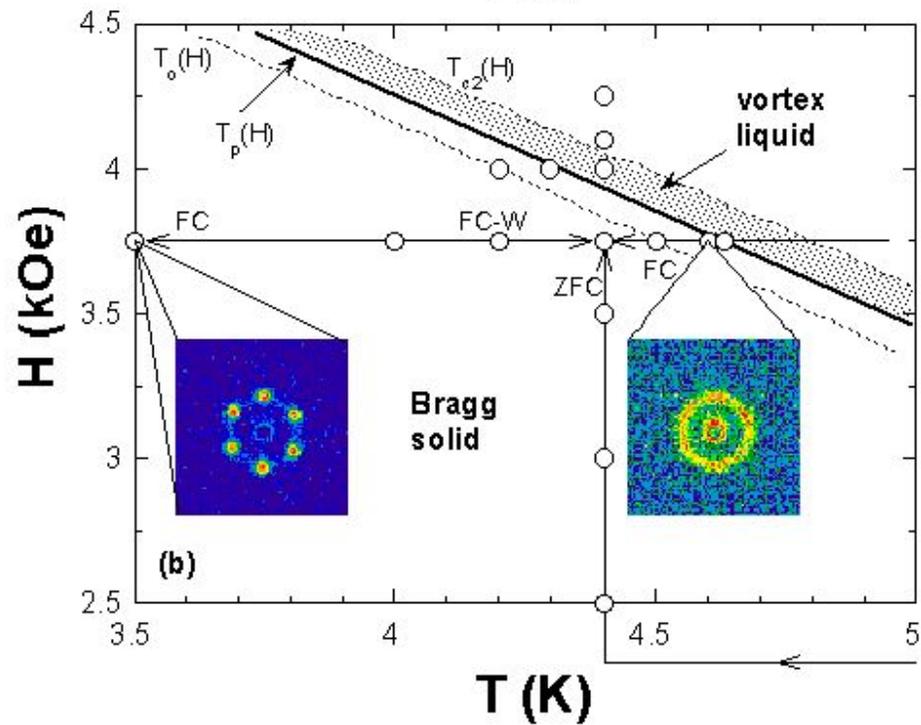
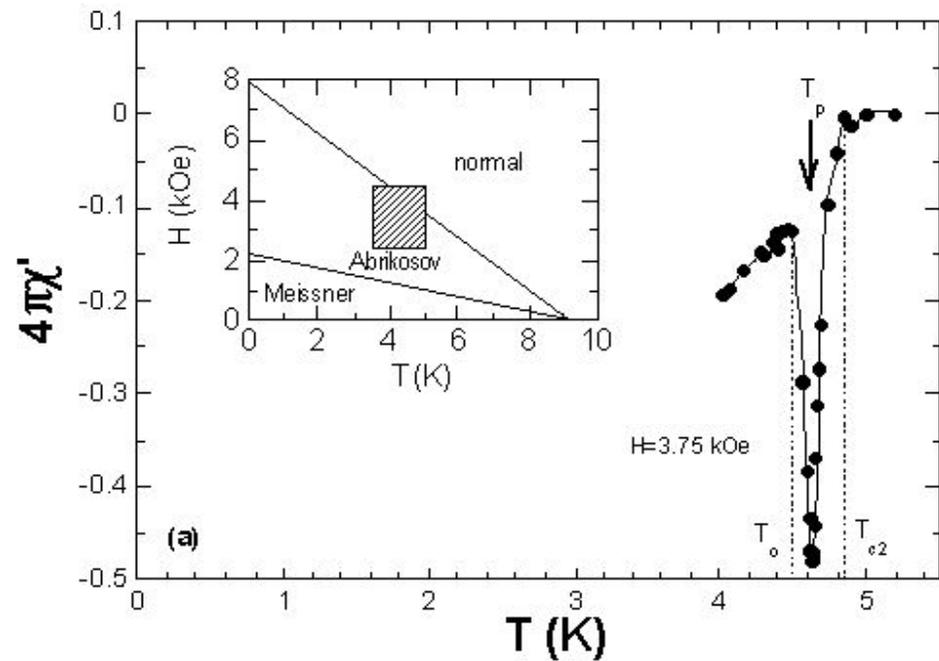
Nb single crystal 99.998%

$\lambda=0.6\text{nm}$, $\Delta\lambda/\lambda=0.11$, $H \parallel \langle 111 \rangle$

NIST Center for Neutron Research



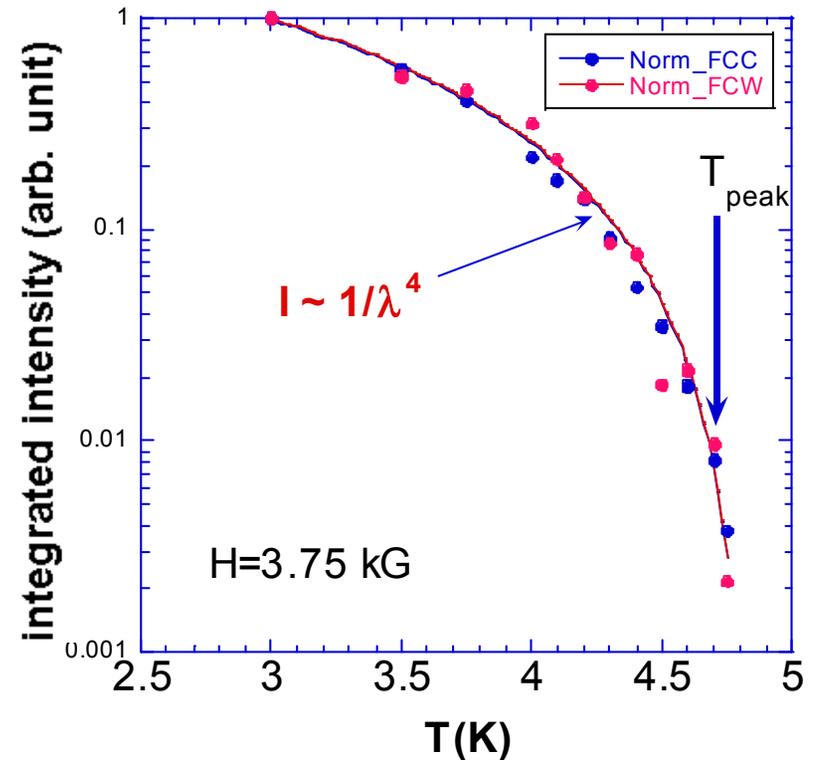
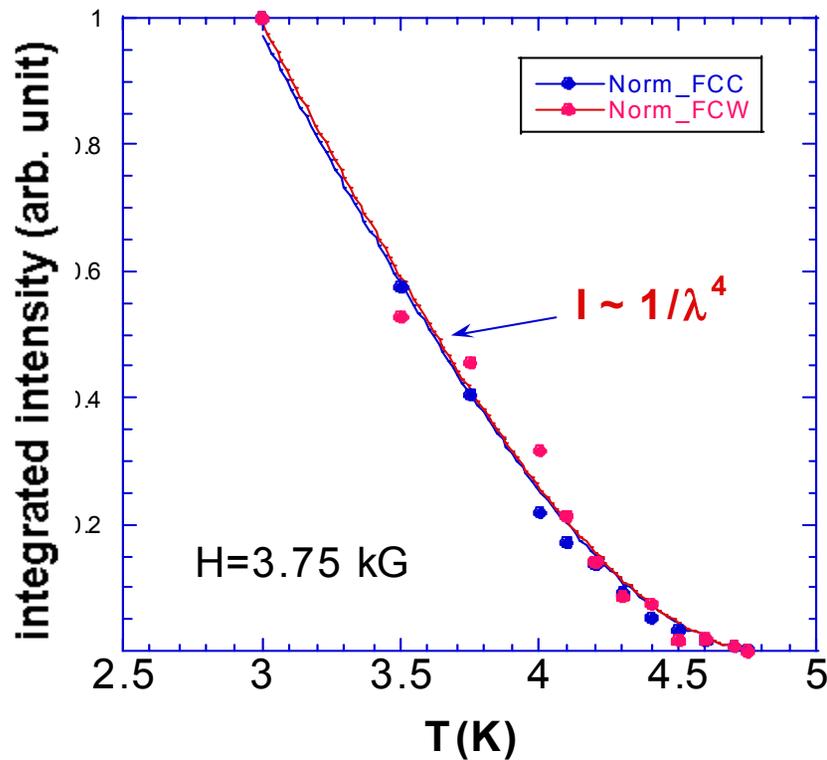
Phase Diagram of Nb



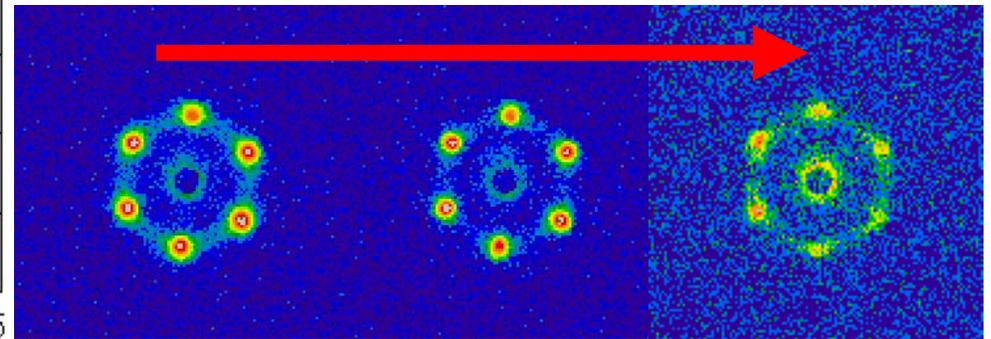
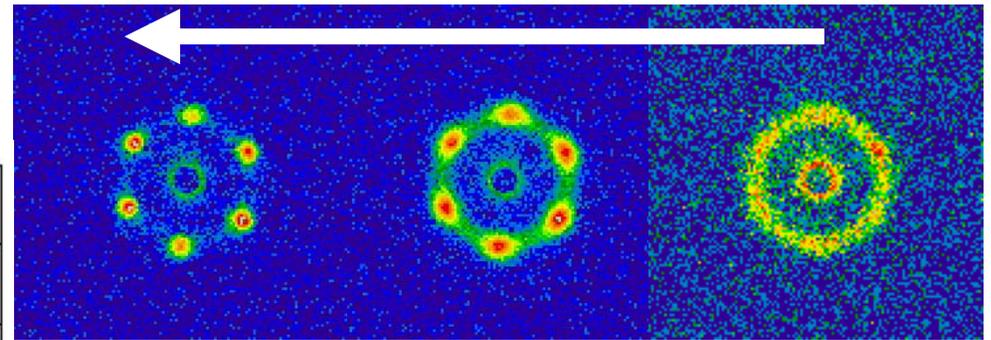
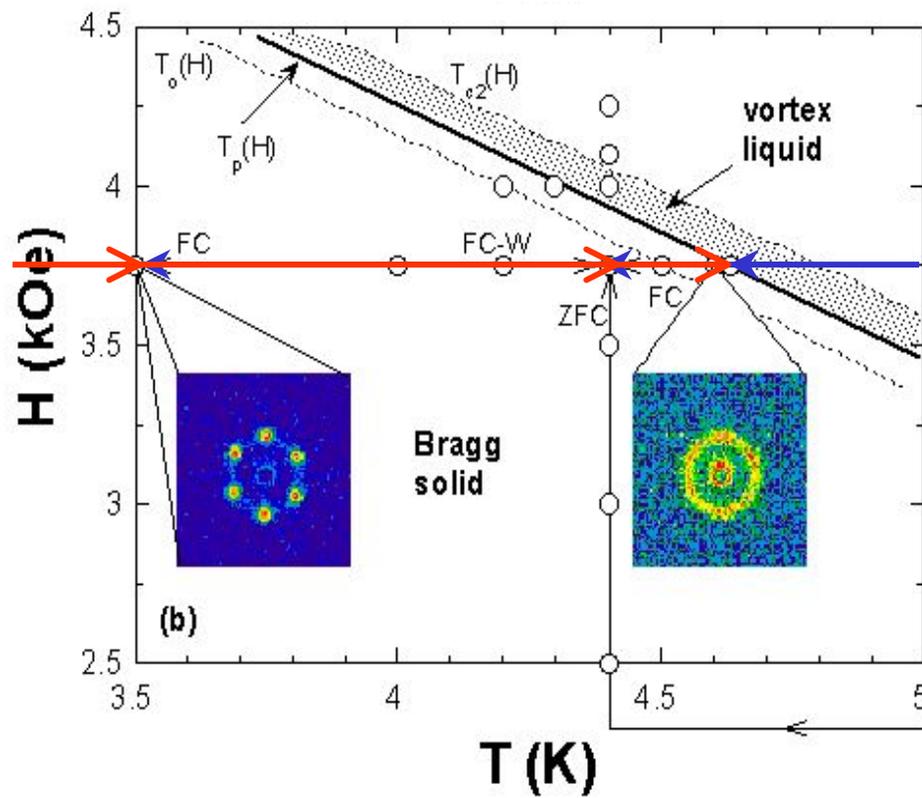
Integrated Intensity

$$I_{hk} = 2\pi\phi \left(\frac{\gamma}{4}\right)^2 \frac{\lambda_n^2}{\Phi_o^2 q_{hk}^2} |F_{hk}|^2 \quad F_{hk} = \frac{B}{1 + \lambda^2 q_{hk}^2}$$

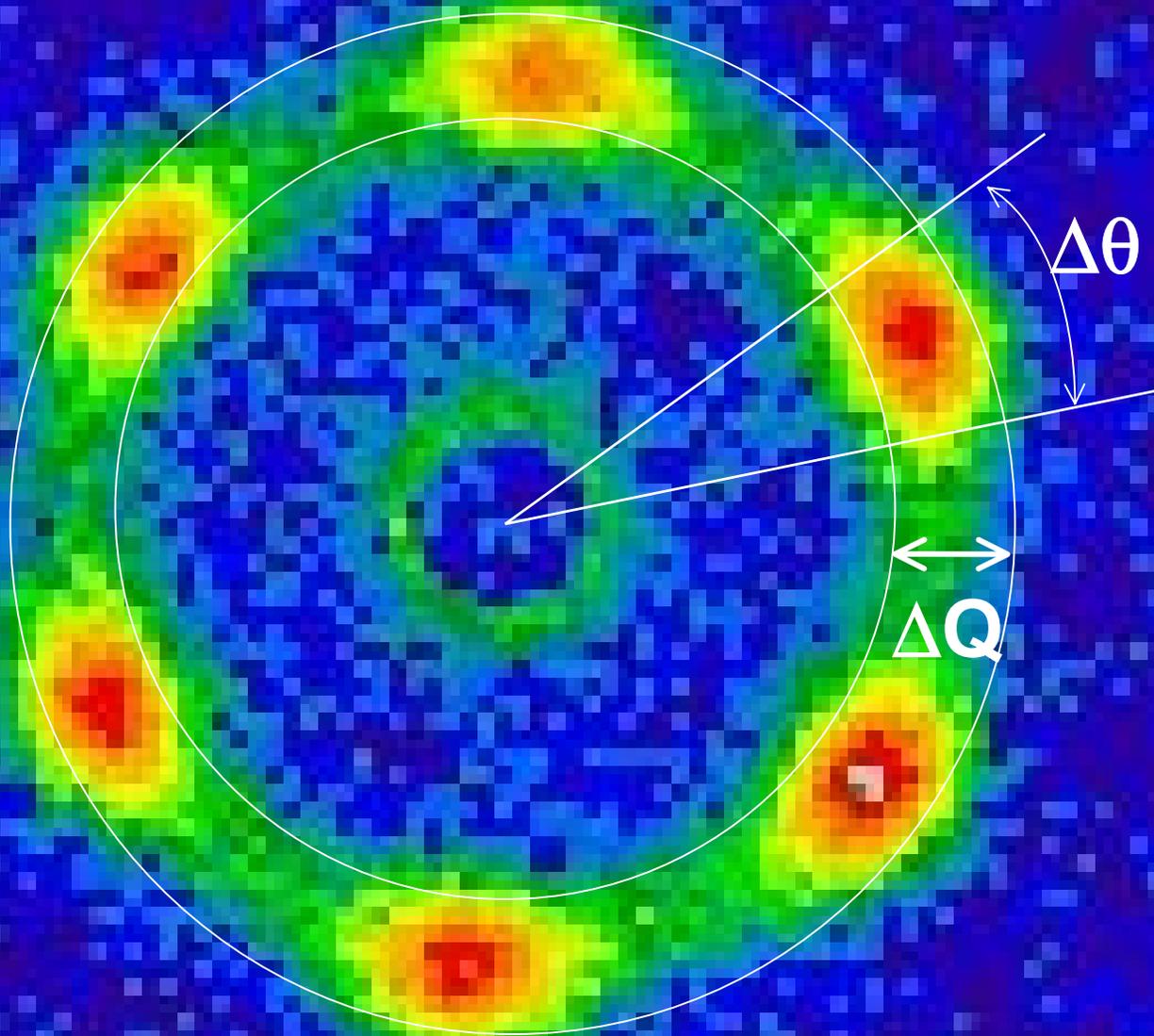
D.K.Christen,F.Tasset,
S.Spooner,H.A.Mook(1977)



Thermal Hysteresis in $S(Q)$

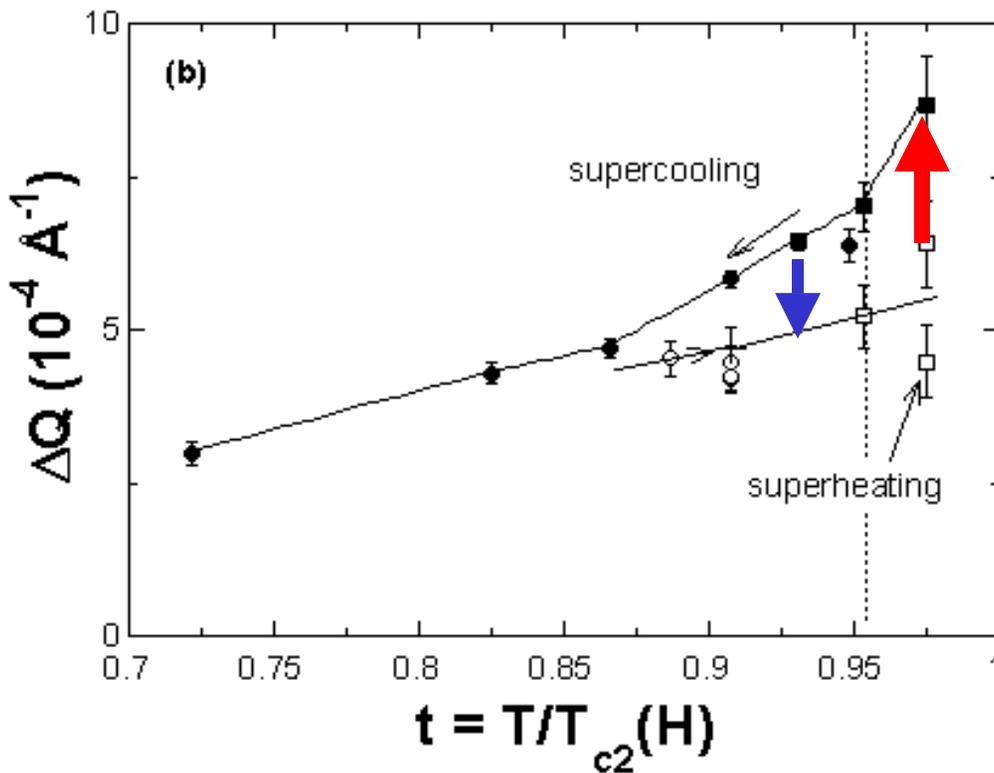
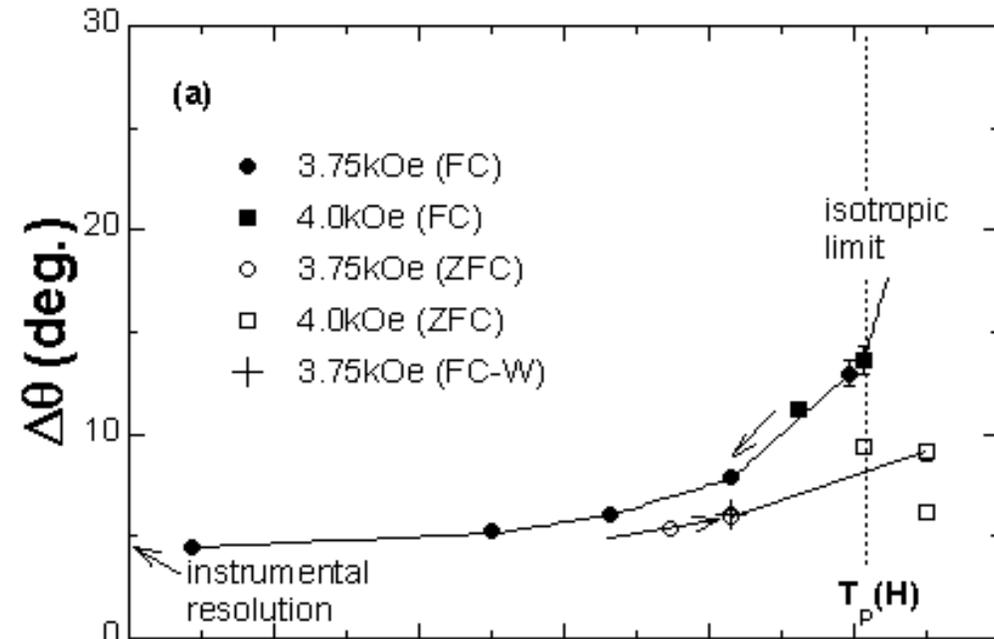


Measurements of order



Orientalional
order

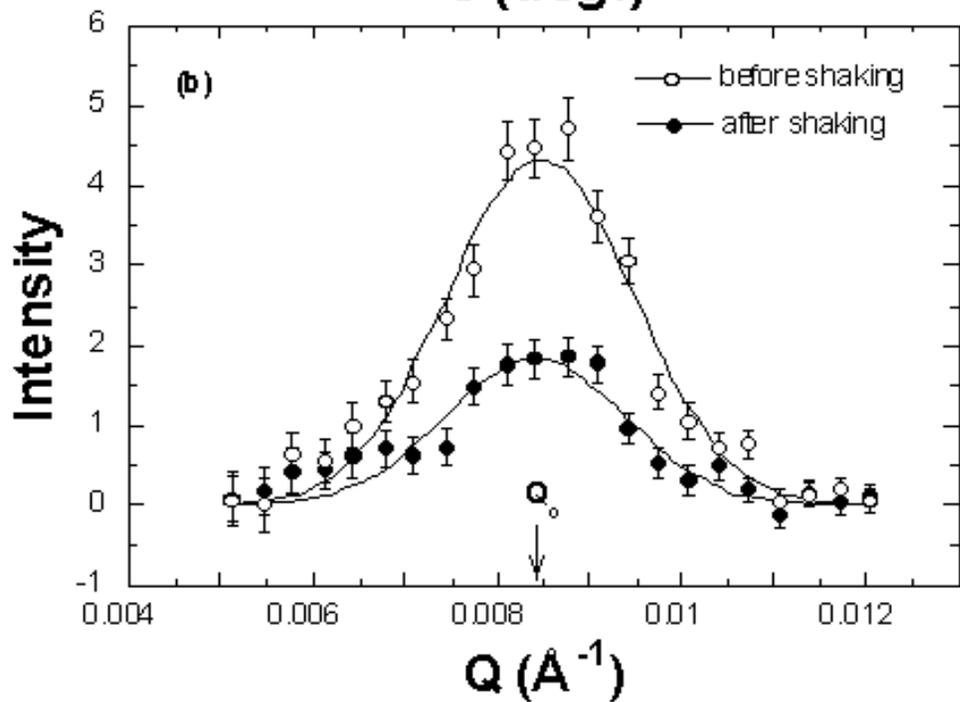
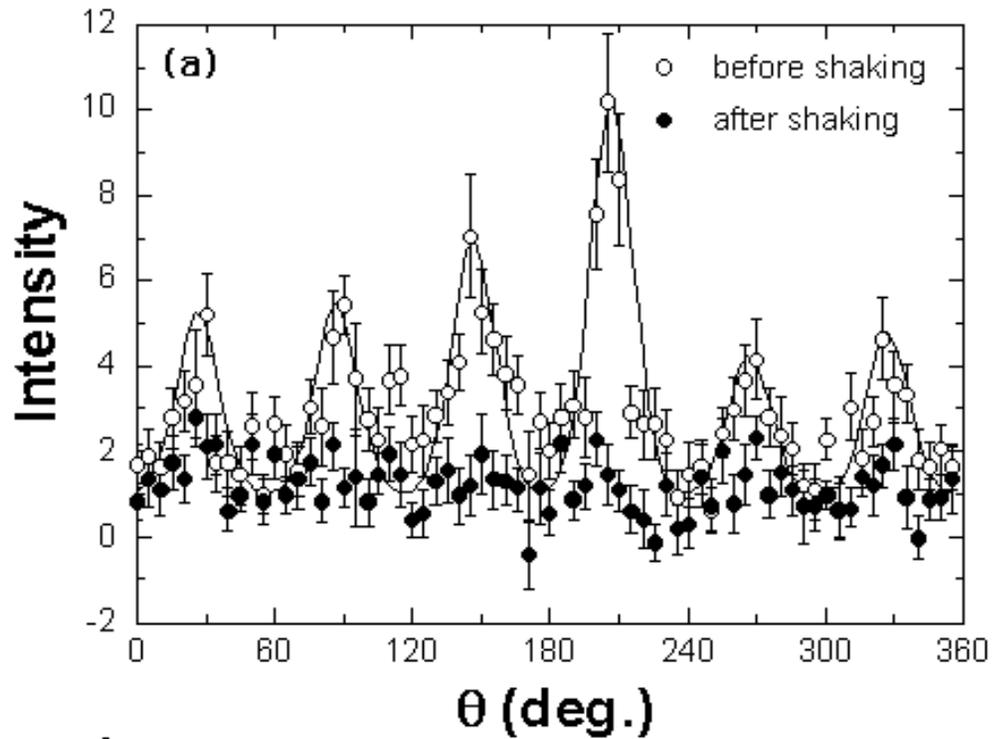
Translational
order



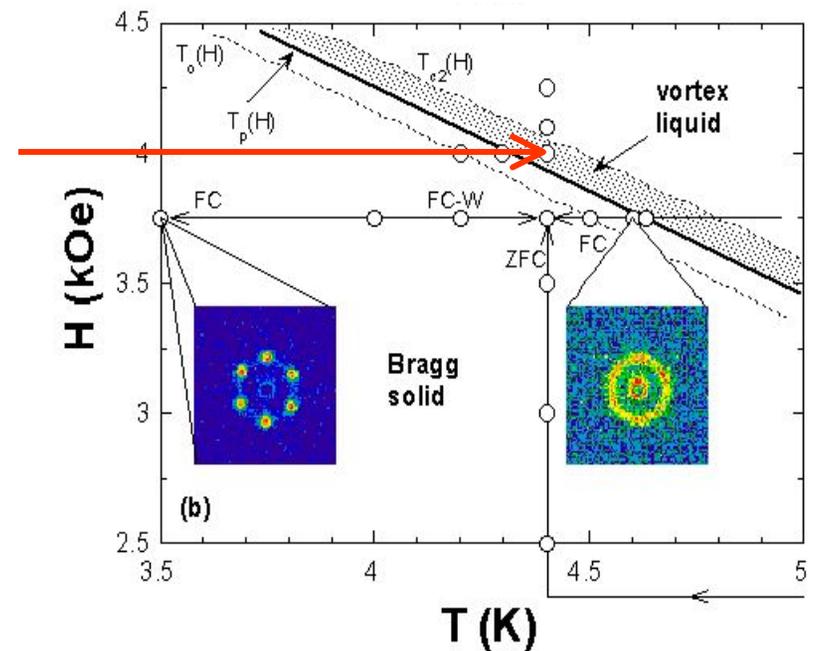
Direct evidence of a solid-liquid transition:
 Simultaneous broadening of Bragg peaks in azimuthal and radial widths

Annealing effects

X.S. Ling et al. PRL 86, 712(2001)



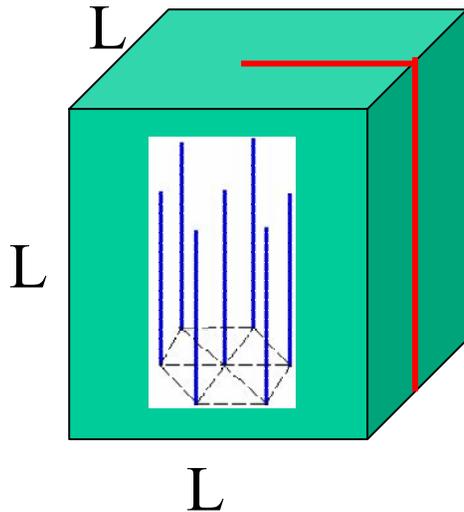
Bragg glass can be superheated, melts upon shaking.



A vortex line solid-liquid transition must be accompanied by a disentanglement-entanglement transition.

D.R. Nelson (1988)

D.R. Nelson, M.C. Marchetti (1990)



Consider the free energy of an edge dislocation in a solid of rigid lines

$$\text{Cost } U = aL \log(L)$$

$$\text{Gain } S = k_B \log(L^2)$$

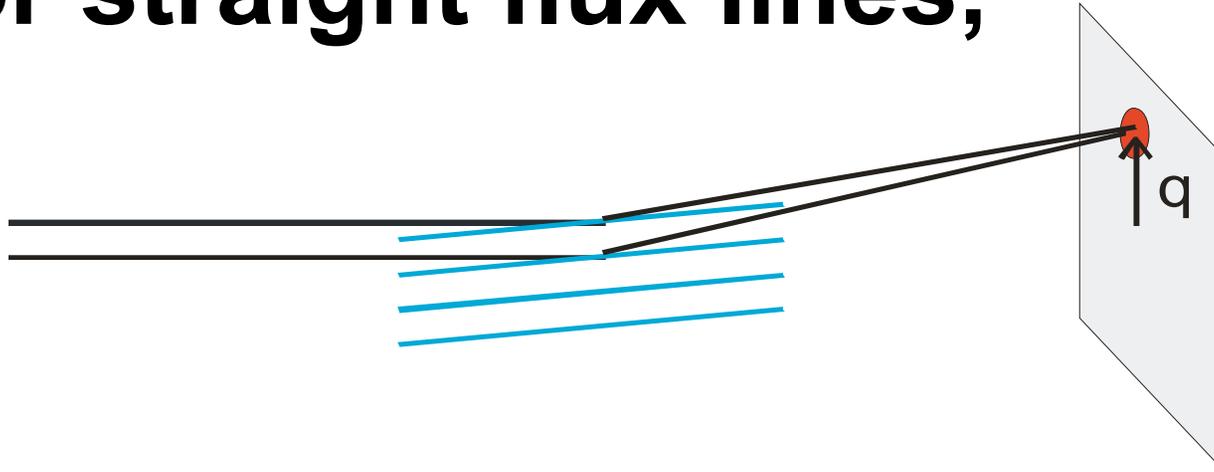
$$F = U - TS = (aL - 2k_B T) \log(L)$$

**In thermodynamic limit, large L, edge dislocations are forbidden.
Rigid-line solids cannot melt.**

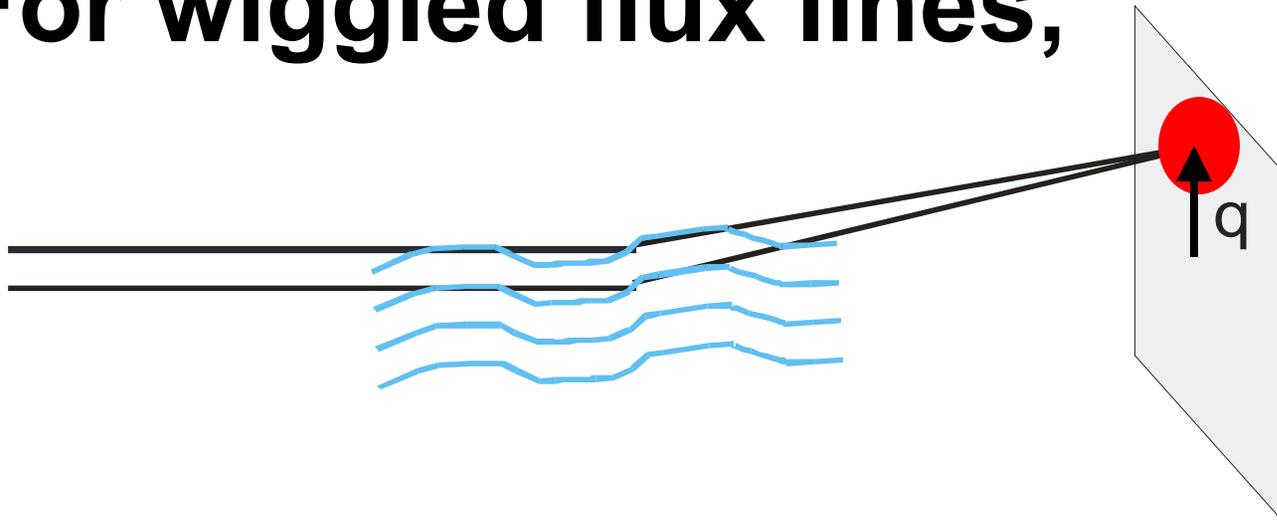
Vortex-line solid melting must have entanglement effects.

Search for the Nelson-Marchetti effect:

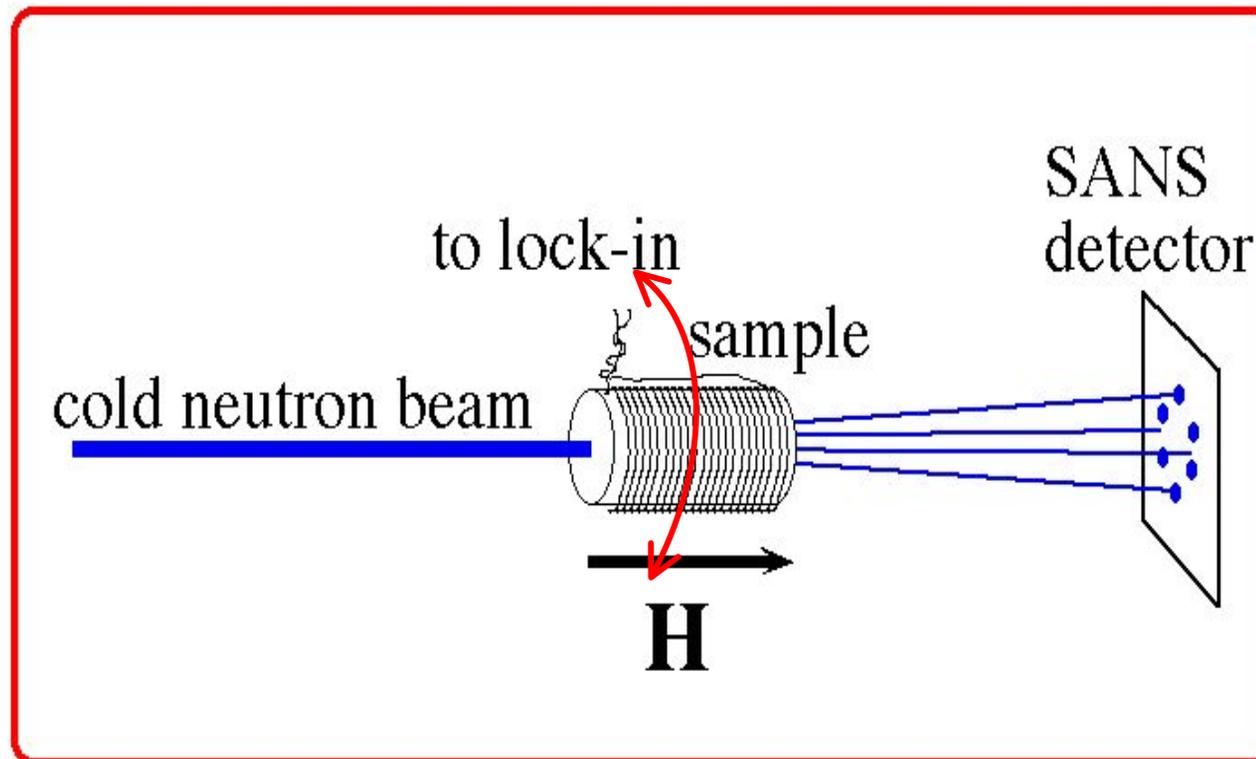
For straight flux lines,

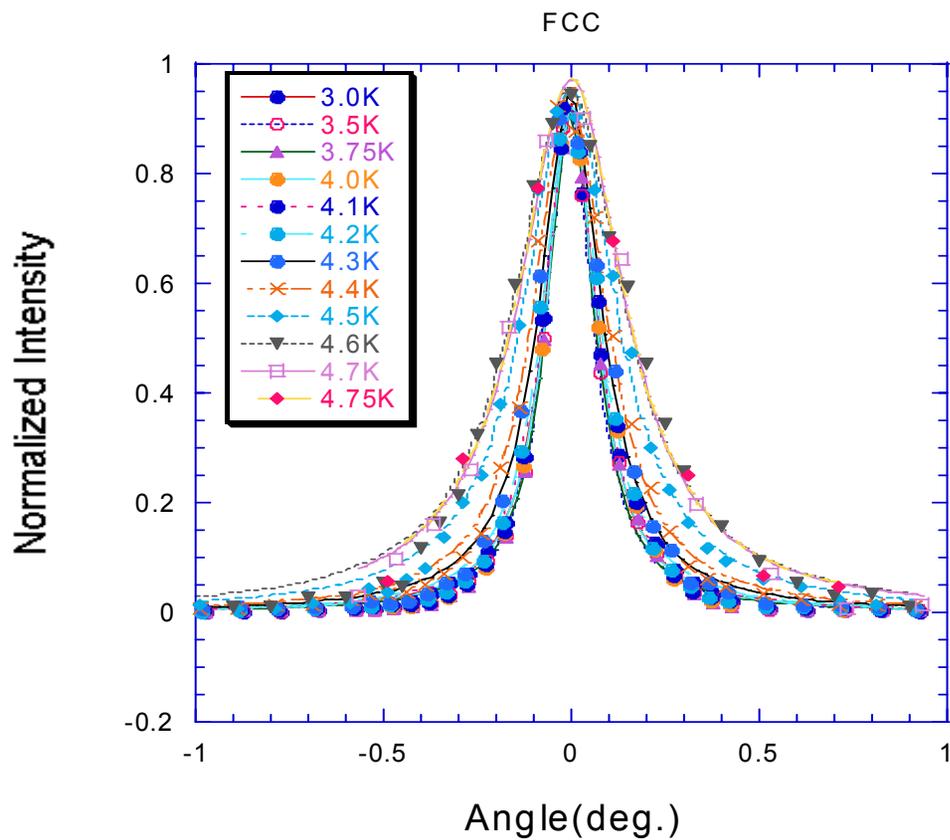


For wiggled flux lines,



Rocking curve widths:
straightness of vortex lines





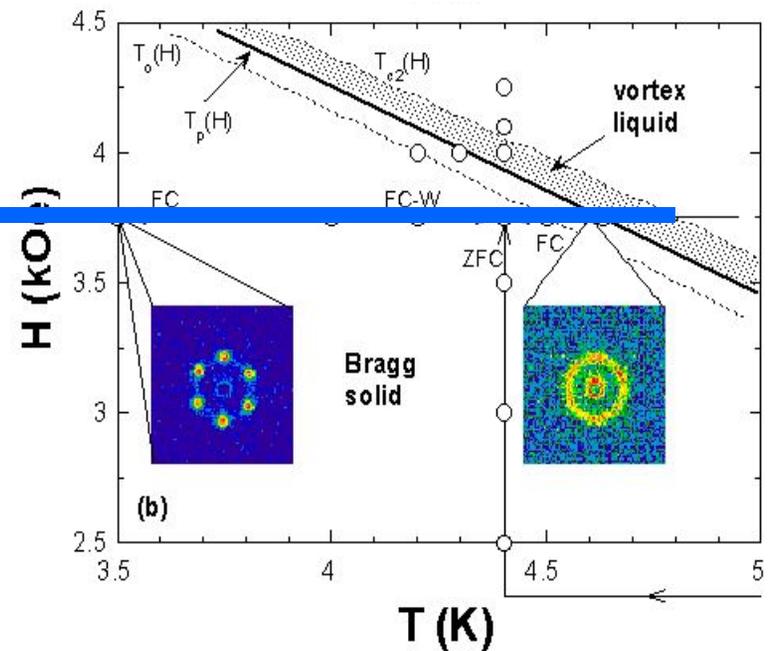
Cooling in field:

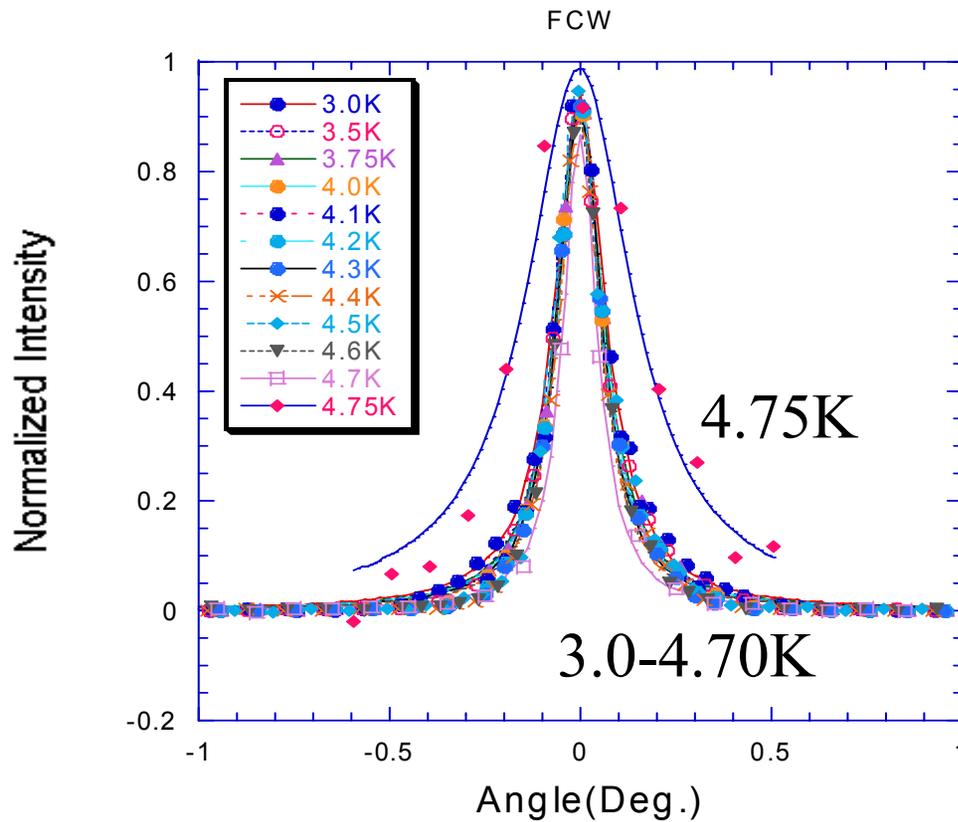
Gradual sharpening of rocking curves:

supercooled phase is made of entangled vortex lines

Such supercooling effects were observed in transport:

Xiao, Andrei et al.
Kes et al.





Warming in field:

Sudden broadening of rocking curves:

Vortex lines remain straight up to $T_p(H)$.

Melting occurs by entanglement.

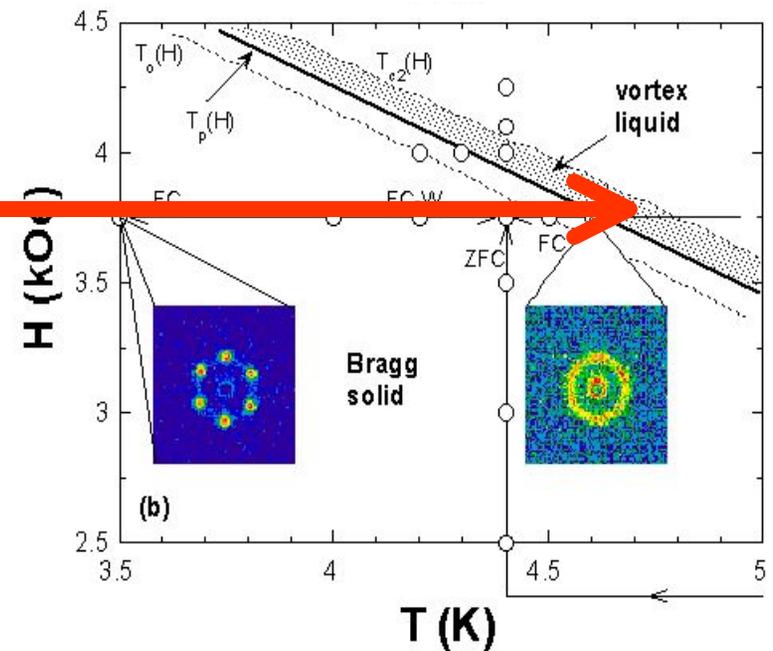
Recent numerical simulations also suggested this effect:

Nonomura, Hu (2001)

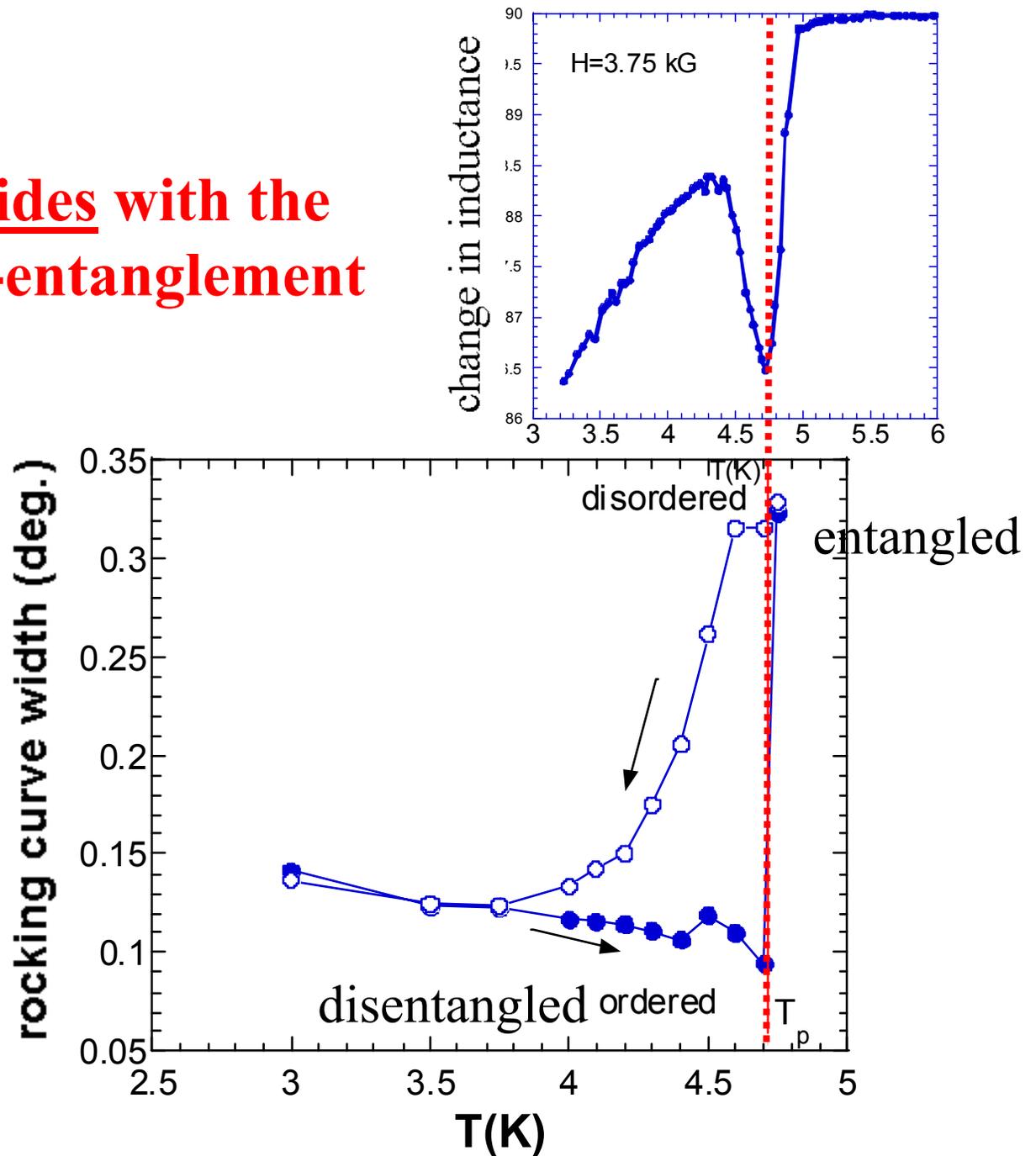
Teitel (2001)

Reichardt (2001)

Kosterlitz (2002)

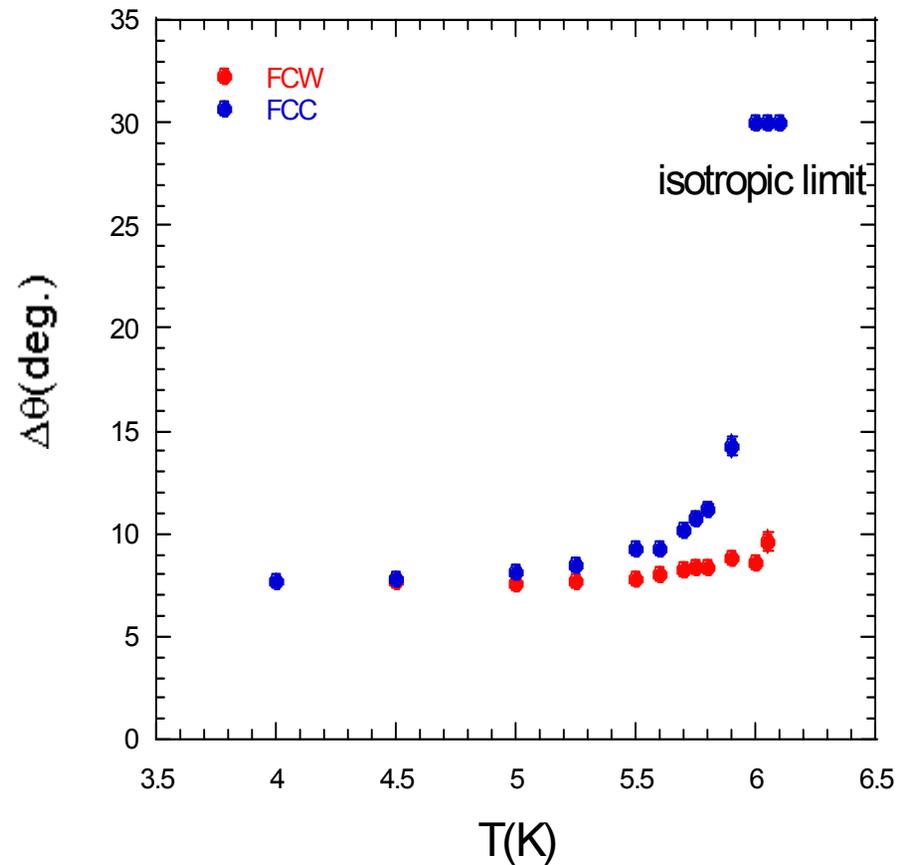


Peak effect coincides with the disentanglement-entanglement transition.

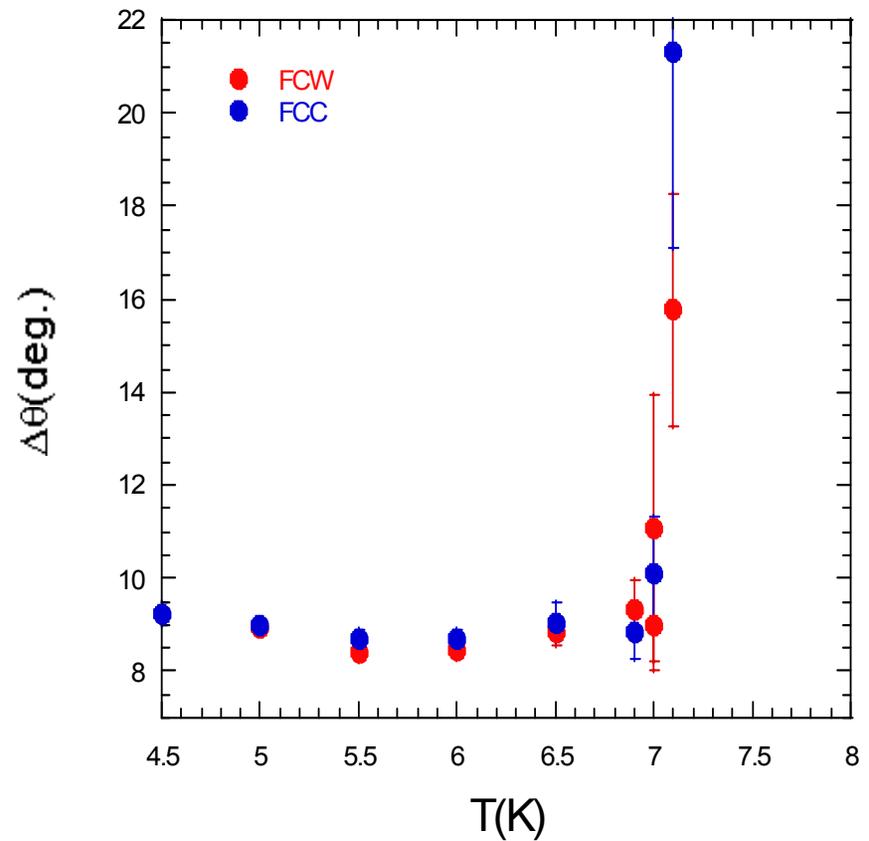


S(Q) hysteresis effect disappears at low H

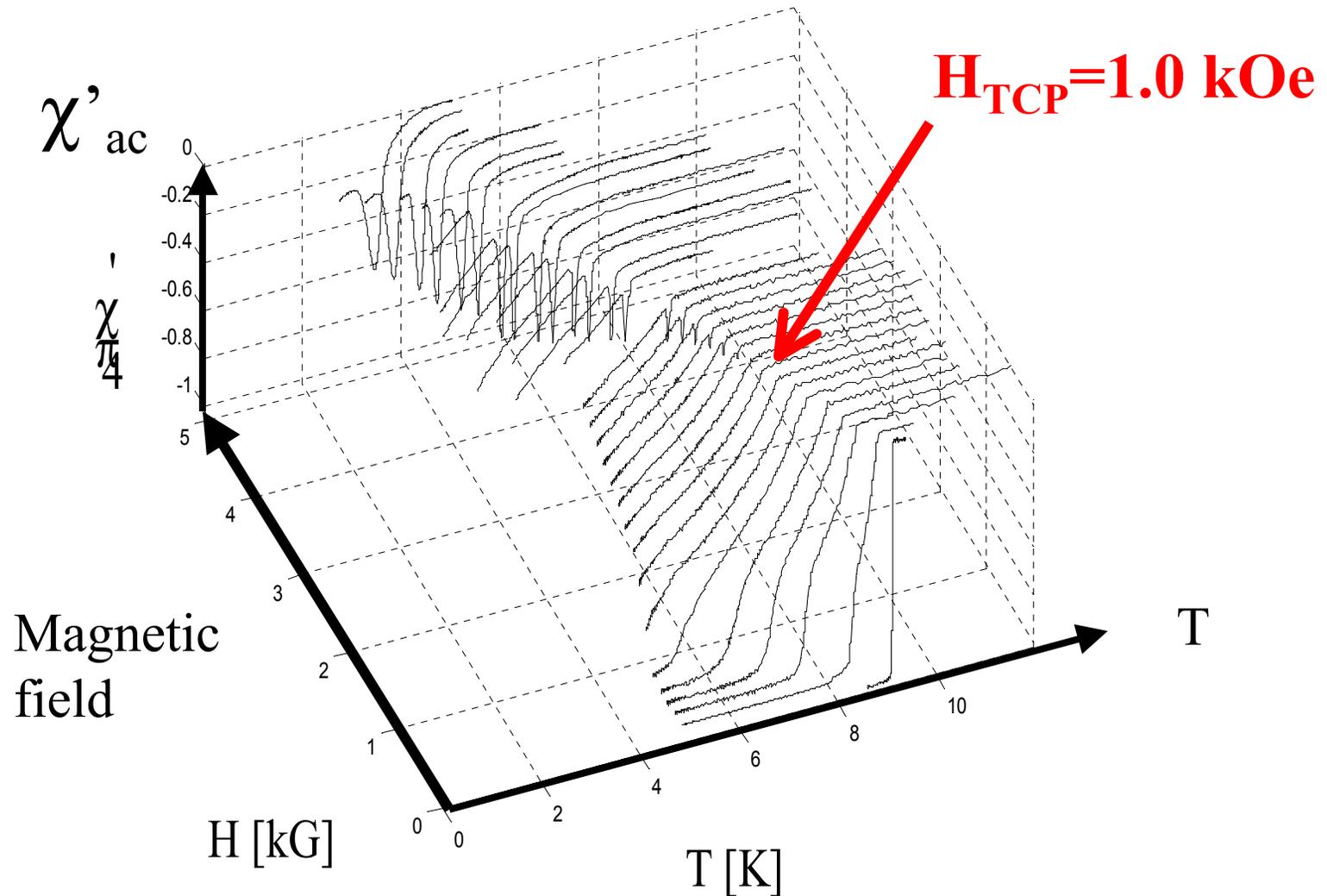
H = 3kG

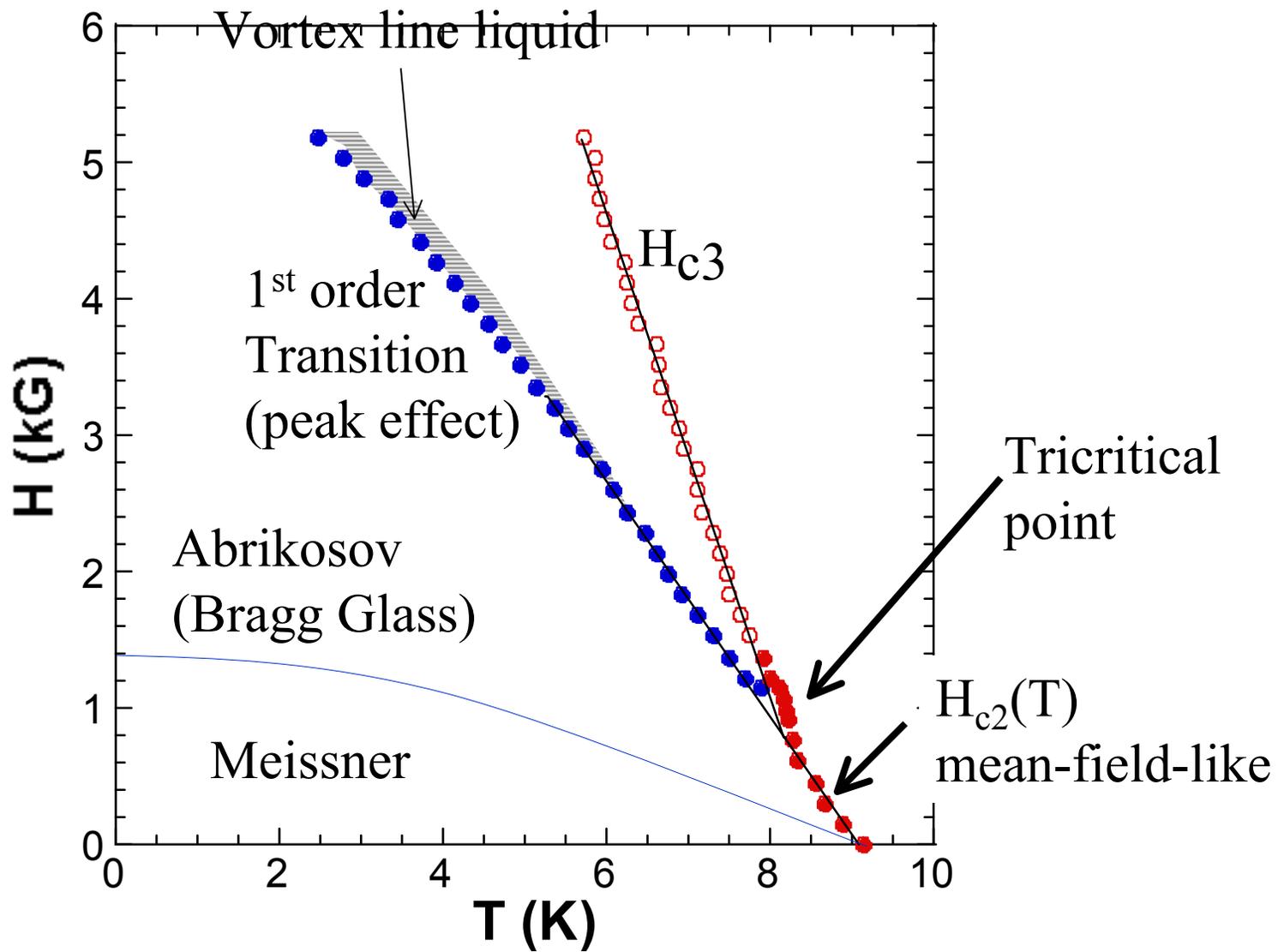


H = 2kG



The peak effect has an end point at low H!





Conclusions:

1. We observed the first direct evidence of a first-order vortex solid-liquid transition at the peak effect, using *in-situ* neutron scattering and ac susceptibility measurements.
2. At low field, the hysteresis of vortex-matter structure factor becomes negligible and correspondingly the peak effect disappears, suggesting the existence of a tri-critical point on the solid-liquid phase boundary.
3. The vortex solid-liquid transition is indeed accompanied by entanglement-disentanglement transition, as predicted by theory (Nelson, 1988).



Sang Ryul Park

Bridget McClain